

Geochemical Modeling to Evaluate Remediation Options for Iron-Laden Mine Discharges

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Summary

Aqueous geochemical tools using PHREEQC have been developed by USGS for OSMRE's "AMDTreat" cost-analysis software:

- ✓ Iron-oxidation kinetics model considers pH-dependent abiotic and biological rate laws plus effects of aeration rate on the pH and concentrations of CO₂ and O₂.
- ✓ Limestone kinetics model considers solution chemistry plus the effects of surface area of limestone fragments.
- ✓ Potential water quality from various treatments can be considered for feasibility and benefits/costs analysis.

TREATMENT OF COAL MINE DRAINAGE



Passive

Active

Increase pH/oxidation
with natural substrates &
microbial activity

Reactions slow

Large area footprint

Low maintenance

Increase pH/oxidation
with aeration &/or
industrial chemicals

Reactions fast, efficient

Moderate area footprint

High maintenance

ACTIVE TREATMENT

28 % – aeration; no chemicals (Ponds)

21 % – caustic soda (NaOH) used

40 % – lime (CaO ; $\text{Ca}(\text{OH})_2$) used

6 % – flocculent or oxidant used

4 % – limestone (CaCO_3) used



PASSIVE TREATMENT

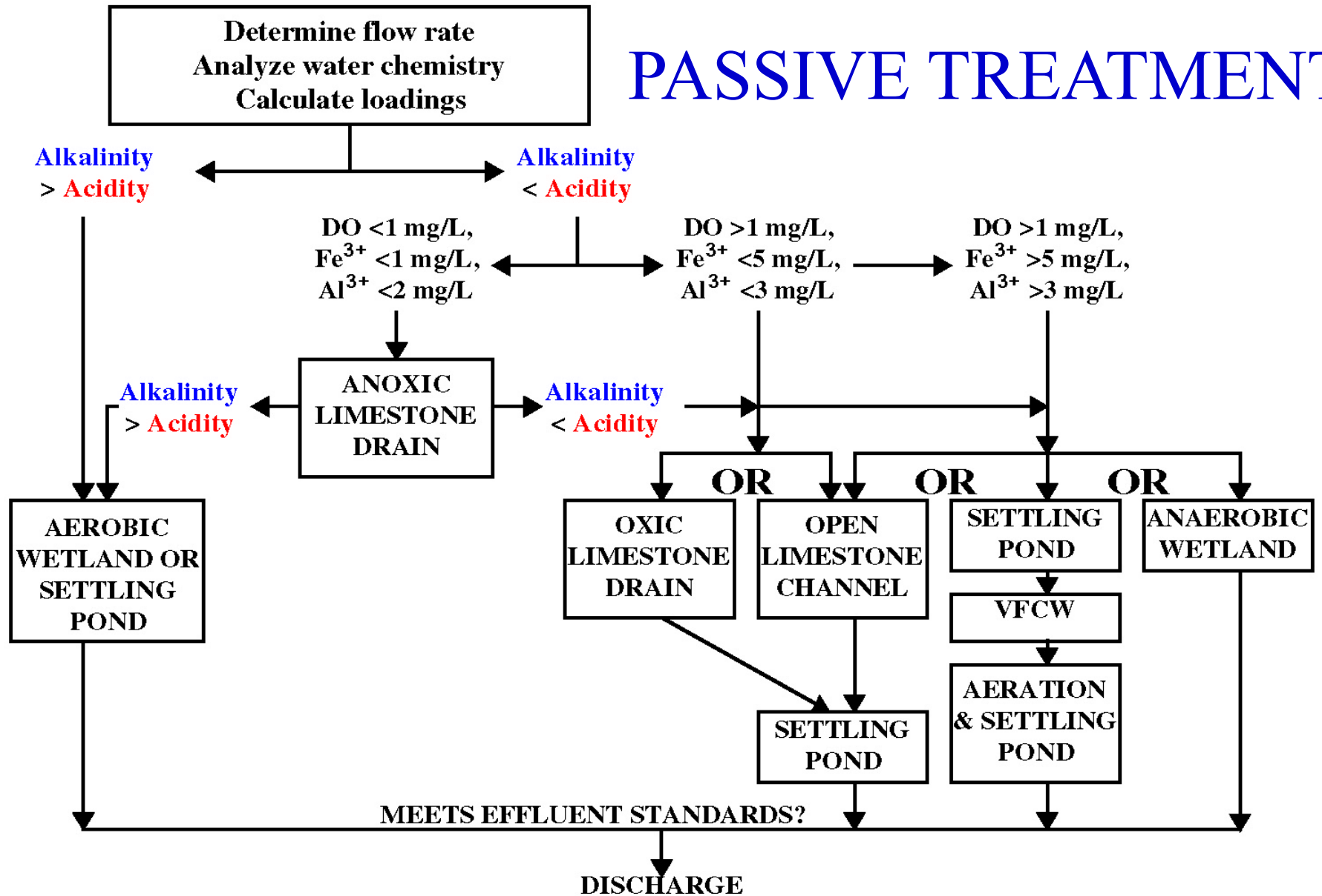


Figure 3. Flow chart for selection of passive treatment alternatives modified from Hedin and others (1994), Skousen and others (1998), and Pennsylvania Department of Environmental Protection (1999). Vertical flow compost wetland (VFCW), also known as SAPS or RAPS.

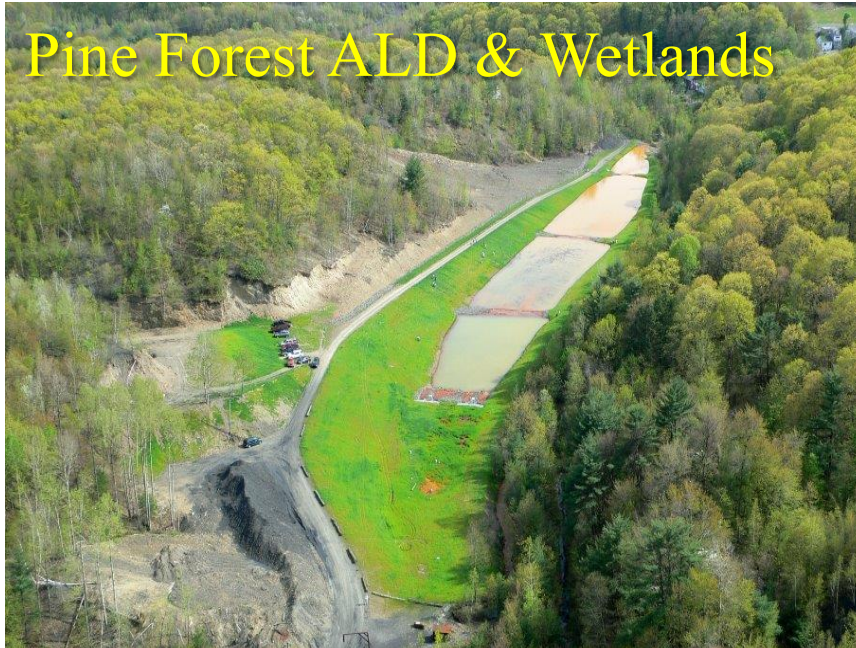
Vertical Flow Limestone Beds
Bell Colliery



PASSIVE TREATMENT

Limestone Dissolution,
O₂ Ingassing,
CO₂ Outgassing,
Fe(II) Oxidation, & Fe(III)
Accumulation

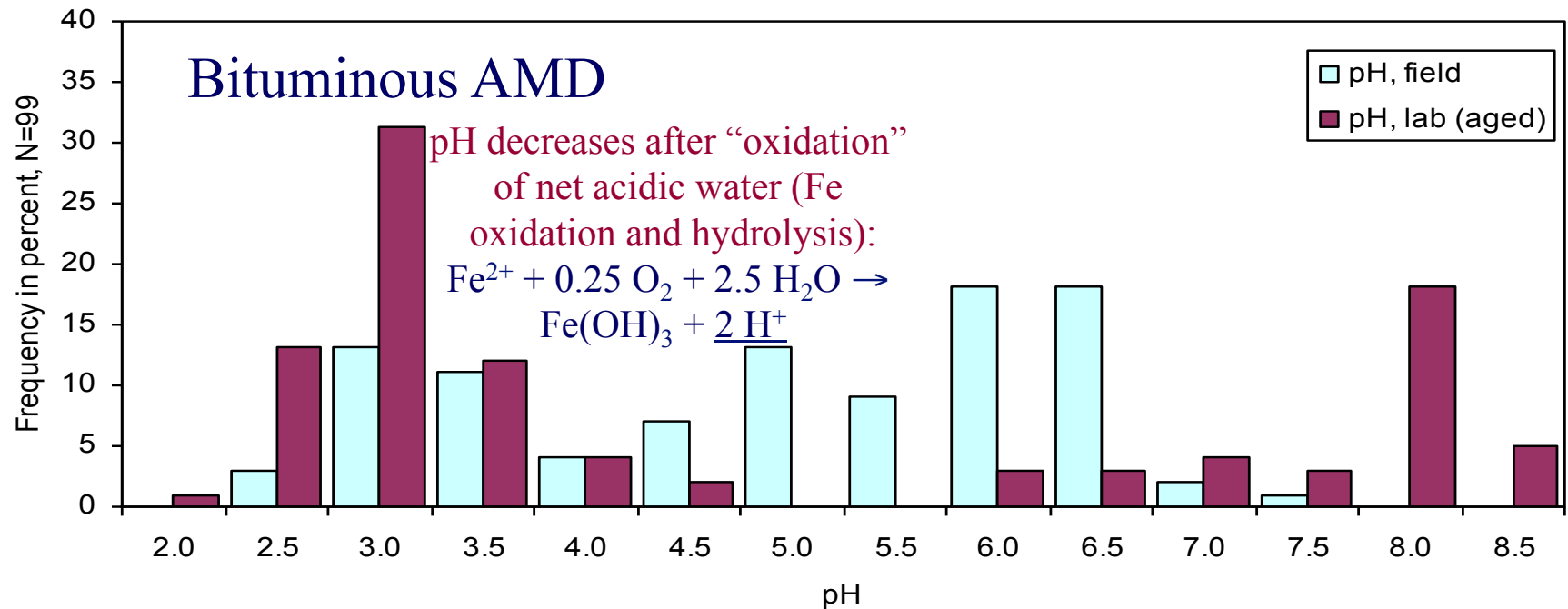
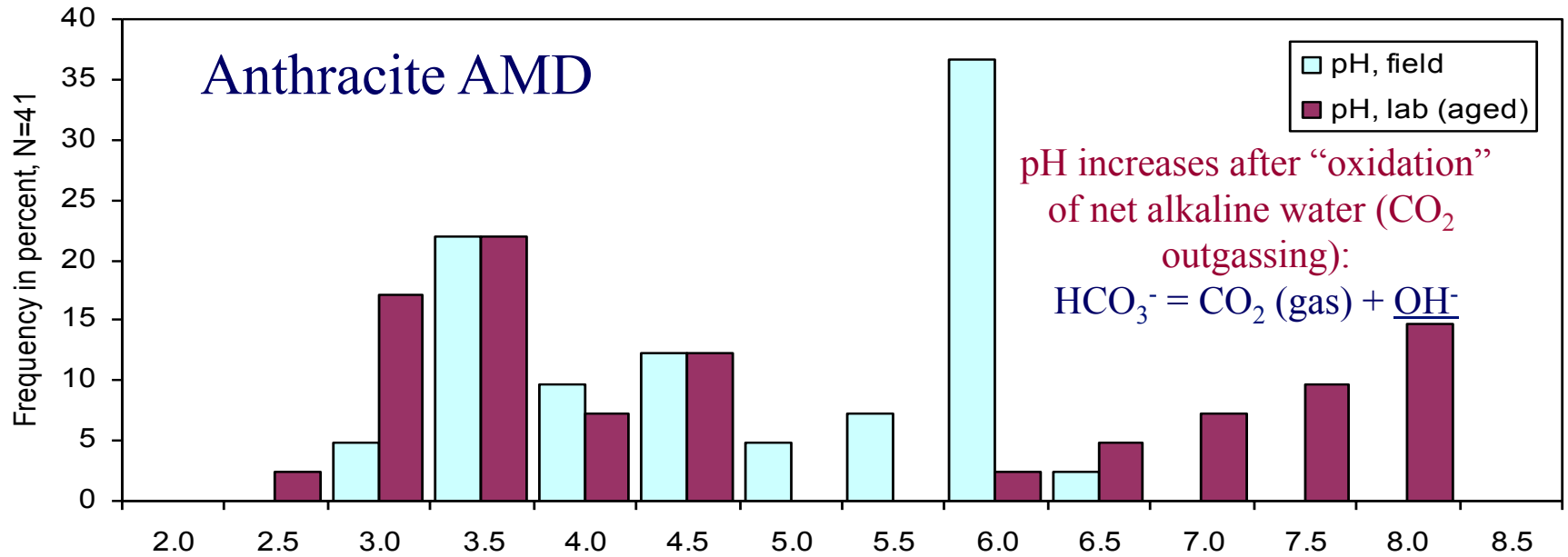
Pine Forest ALD & Wetlands

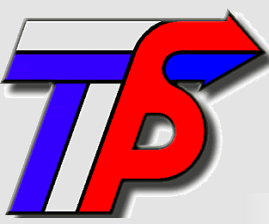


Silver Creek Wetlands



BIMODAL pH FREQUENCY DISTRIBUTION





“PHREEQ-N-AMDTREAT”

<http://amd.osmre.gov/>



AMDTREAT



Take the Tutorial

[DOI HOME](#) [OSMRE HOME](#) [AR HOME](#) [TIPS HOME](#) [SITEMAP](#)

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AMDTREAT 5.0.2 PLUS NOW AVAILABLE!

AMDTreat 5.0.2 Plus corrects minor convergence issues identified during case study tests performed by the developers.

Enhancements to Version 5 of AMDTreat include incorporation of the geochemical modeling capabilities of the U.S. Geological Survey's (USGS) PHREEQ computer program to model titrations and enhancement to the oxidant tool.

For additional information, please contact [Brent Means](#) or [Omar Beckford](#).

WHAT IS AMDTREAT?

AMDTreat (Pronounced: am'-D-treat or A-M-D-treat.), a member of OSMRE's *Technical Innovation and Professional Services (TIPS) suite of software*, is a computer application for estimating abatement costs for pollutional mine drainage, commonly referred to as Acid Mine Drainage or AMD. (Also Acid Rock Drainage or ARD.) The current version of AMDTreat is v5.0.2 Plus. AMDTreat can assist a user in estimating costs to abate water pollution using a variety of passive and chemical treatment types; including, vertical flow ponds, anoxic limestone drains, anaerobic wetlands, aerobic wetlands, bio reactors, manganese removal beds, limestone beds, oxic limestone channels, caustic soda, hydrated lime, pebble quicklime, ammonia, oxidation chemicals, and soda ash treatment systems. The acid mine drainage abatement cost model provides over 400 user modifiable variables in modeling costs for treatment facility construction, excavation, revegetation, piping, road construction, land acquisition, system maintenance, labor, water sampling, design, surveying, pumping, sludge removal, chemical consumption, clearing and grubbing, mechanical aeration, and ditching. AMDTreat also contains several financial and scientific tools to help select and plan treatment systems. These tools include a long-term financial forecasting module, an acidity calculator, a sulfate reduction calculator, a Langelier saturation index calculator, a mass balance calculator, a passive treatment alkalinity calculator, an abiotic homogeneous Fe²⁺ oxidation calculator, a biotic homogeneous Fe²⁺ oxidation calculator, an oxidation tool, and a metric conversion tool.

AMDTreat is a computer application for estimating abatement costs for AMD (acidic or alkaline mine drainage).

AMDTreat is maintained by OSMRE.

The current version of AMDTreat 5.0+ is being recoded from FoxPro to C++ to facilitate its use on computer systems running Windows 10. The PHREEQC geochemical models described below will be incorporated to run with the recoded program.

AMDTREAT 5.0+

- With the “PHREEQC chemical titration tool,” AMDTreat 5.0+ has capability to estimate:
 - ✓ Quantity and cost of caustic chemicals to attain a target pH (without and with pre-aeration);
 - ✓ Chemistry of treated effluent after reactions; and
 - ✓ Volume of sludge produced as the sum of precipitated metal hydroxides plus unreacted chemicals.

AMDTREAT 5.0+

- PHREEQ-N-AMDTreat “chemical titration tool” accurately relates caustic addition, pH, and metals solubility ... but
 - ✓ assumes instantaneous, complete reactions without consideration of kinetics of gas exchange rates; and
 - ✓ ignores effects of changing pH on iron oxidation rate.

AMDTreat 5.0+ Caustic Addition— St. Michaels Discharge



AMDTreat 5.0+.lnk

Escape Presentation

Costs

Passive Treatment		A	S	
Vertical Flow Pond	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Anoxic Limestone Drain	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Anaerobic Wetlands	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Aerobic Wetlands	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Mn Removal Beds	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Oxic Limestone Channel	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Limestone Bed	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
BIO Reactor	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Passive Subtotal:				\$0
Active Treatment		A	S	
Caustic Soda	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Hydrated Lime	<input checked="" type="checkbox"/>	<input type="checkbox"/>	X	\$759,574
Pebble Quick Lime	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Ammonia	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Oxidant Capital Cost	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Soda Ash	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Active Subtotal:				\$759,574
Ancillary Cost		A	S	
Ponds	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Roads	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Land Access	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Ditching	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Engineering Cost	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Ancillary Subtotal:				\$0
Other Cost (Capital Cost)				\$0
Total Capital Cost:				\$759,574

Annual Costs		A	S	
Sampling	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Labor	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Maintenance	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Pumping	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Chemical Cost	<input checked="" type="checkbox"/>	<input type="checkbox"/>	X	\$973,674
Oxidant Chem Cost	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Sludge Removal	<input type="checkbox"/>	<input type="checkbox"/>	X	\$0
Other Cost (Annual Cost)				\$0
Land Access (Annual Cost)				\$0
Total Annual Cost:				\$973,674
Annual Cost per 1000 Gal of H2O Treated				\$0.243
Other Costs		A	S	
Other Costs	<input type="checkbox"/>	<input type="checkbox"/>	X	

Project
St Michaels
Company
USGS, Cravotta
Site Name
Hydrated Lime No Aeration
Run Date
04/07/2017
Comments
Maelstrom data from Brent Means

Water Quality

Design Flow	7600.00	gpm
Typical Flow**	7600.00	gpm
Total Iron	136.00	mg/L
Est. Ferrous Iron	135.99	mg/L
Aluminum	0.35	mg/L
Manganese	4.10	mg/L
pH	5.72	su
Alkalinity as CaCO3	62.80	mg/L
Est. TIC as C	62.00	mg/L
Calculate Net Acidity		
Enter Acidity manually		
Acidity as CaCO3	205.00	mg/L
Sulfate	1100.00	mg/L
Chloride	38.70	mg/L
Calcium	212.00	mg/L
Magnesium	85.20	mg/L
Sodium	25.50	mg/L
Water Temperature	15.40	C
Specific Conductivity	1879.00	uS/cm
Total Dissolved Solids	1742.00	mg/L
Dissolved Oxygen	0.01	mg/L
Typical Acid Loading	3,413.5	tons/yr

Red indicates information used in critical calculations
 Black indicates optional parameters
 Blue indicates information used by PHREEQ
 ** Typical Flow should represent the flow (e.g. median) used to estimate chemical reagent and sludge amounts

Report



EXIT



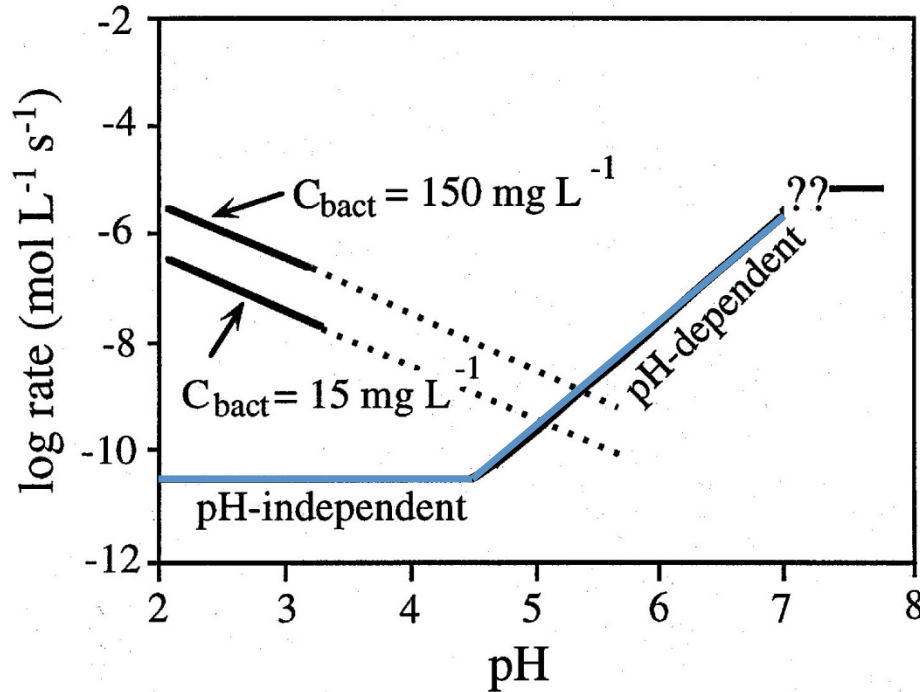
“New” PHREEQC Kinetics Models for AMDTreat 5.0+

- ✓ FeII oxidation model that utilizes established rate equations for gas exchange and pH-dependent iron oxidation and that can be associated with commonly used aeration devices/steps (including decarbonation);
- ✓ Limestone dissolution model that utilizes established rate equation for calcite dissolution and that can be adjusted for surface area of commonly used aggregate particle sizes.

KINETICS OF IRON OXIDATION – pH & GAS EXCHANGE EFFECTS



Iron Oxidation Kinetics are pH Dependent (abiotic and microbial processes can be involved)



EXPLANATION



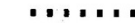
-  Abiotic; rates to pH 7 from STUMM and MORGAN (1996)
- ?? Uncertain transition to pH-independence
-  Bacterial; rates to pH 3 from PESIC *et al.* (1989)
-  Extrapolation of PESIC *et al.* (1989) rates

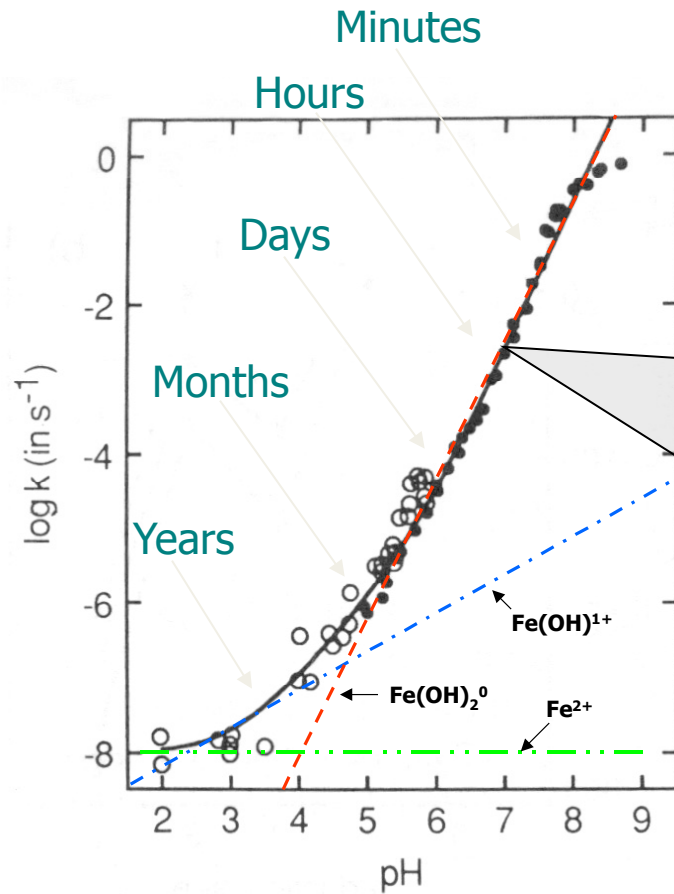
Fig. 3. Rate of Fe(II) oxidation versus pH based on abiotic and biological rate laws (Kirby et al., 1999)

** C_{bact} is concentration of iron-oxidizing bacteria, in mg/L, expressed as dry weight of bacteria ($2.8E-13$ g/cell or $2.8E-10$ mg/cell).

The AMDTreat Fell oxidation kinetic model uses most probable number of iron-oxidizing bacteria per liter (MPNbact).

$C_{bact} = 150$ mg/L is equivalent to $MPNbact = 5.3E11$, where $C_{bact} = MPNbact \cdot (2.8E-10)$.

Abiotic Homogeneous Fe(II) Oxidation Rate (model emphasizes pH)



Between pH 5 and 8 the Fe(II) oxidation rate increases by 100x for each pH unit increase.*

At a given pH, the rate increases by 10x for a 15 °C increase. Using the activation energy of 23 kcal/mol with the Arrhenius equation, the rate can be adjusted for temperature.

*Extrapolation of homogeneous rate law:

$$-d[\text{Fe(II)}]/dt = k_1 \cdot [\text{Fe(II)}] \cdot [\text{O}_2] \cdot [\text{H}^+]^{-2}$$

$$k_1 = 3 \times 10^{-12} \text{ mol/L/min}$$

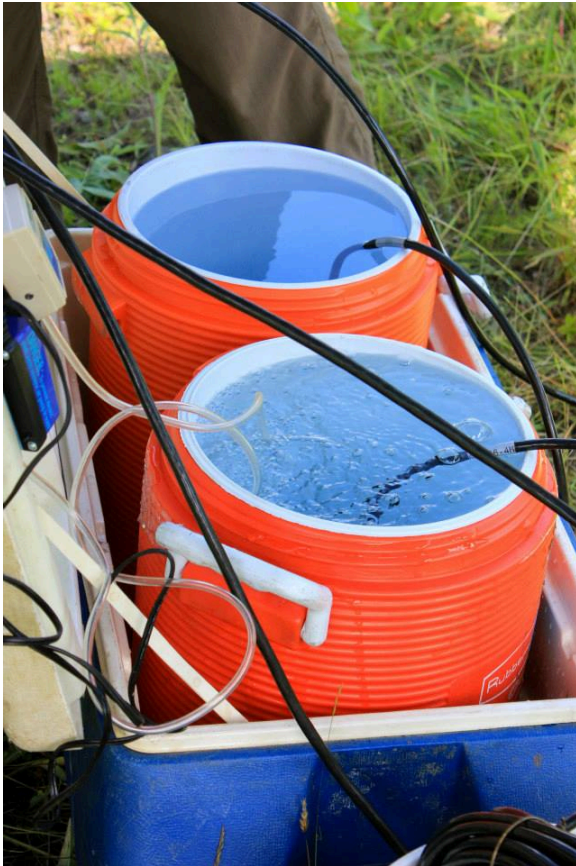
$$\log k_{T_1} = \log k_{T_2} + E_a / (2.303 \cdot R) \cdot (1/T_2 - 1/T_1)$$

At $[\text{O}_2] = 0.26 \text{ mM}$ ($p\text{O}_2 = 0.21 \text{ atm}$) and 25°C .
 Open circles (o) from Singer & Stumm (1970),
 and solid circles (•) from Millero et al. (1987).

Dashed lines are estimated rates for the various dissolved Fe(II) species.

Effects of O_2 Ingassing and CO_2 Outgassing on pH and Fe(II) Oxidation Rates

Batch Aeration Tests at Oak Hill Boreholes (summer 2013)



Control Not Aerated



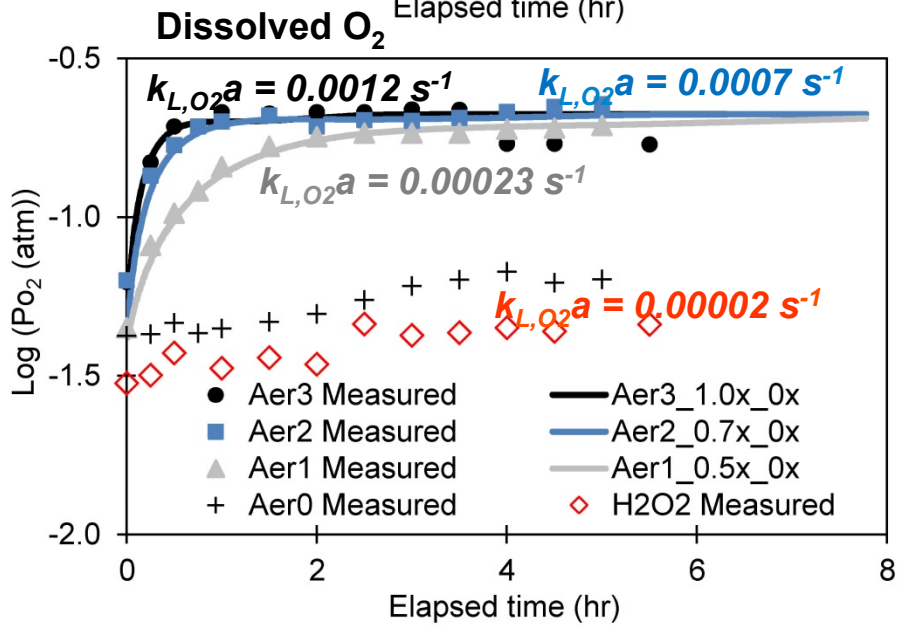
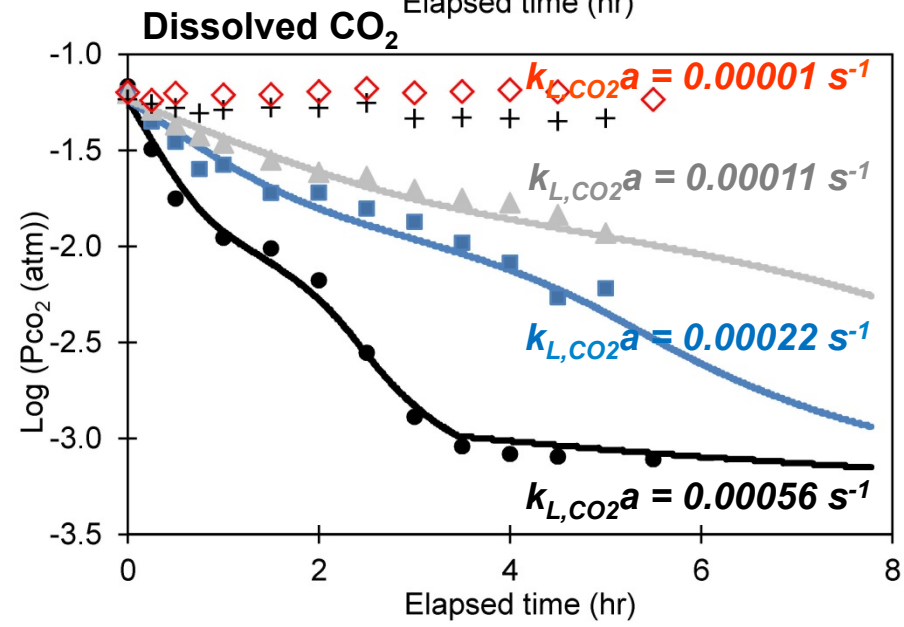
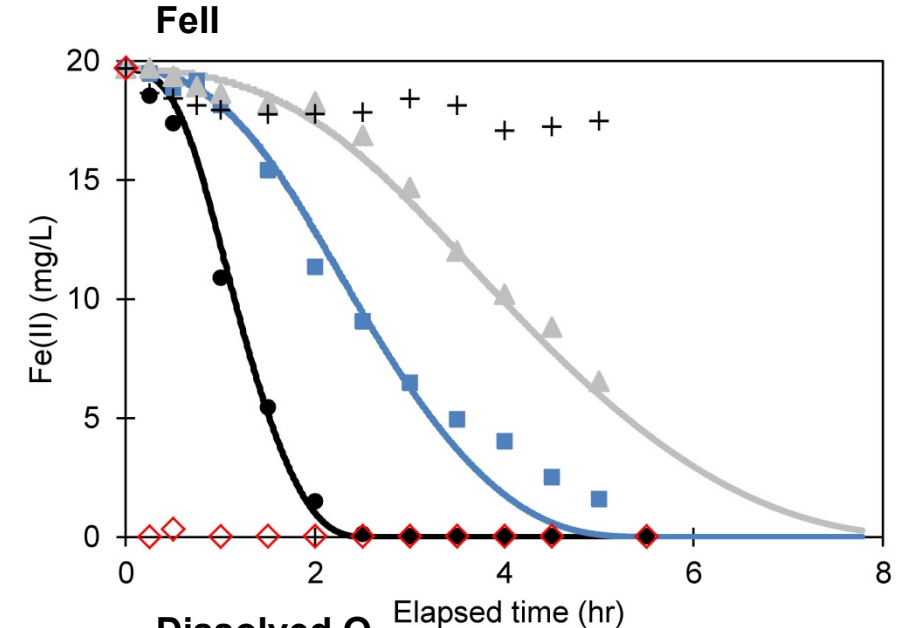
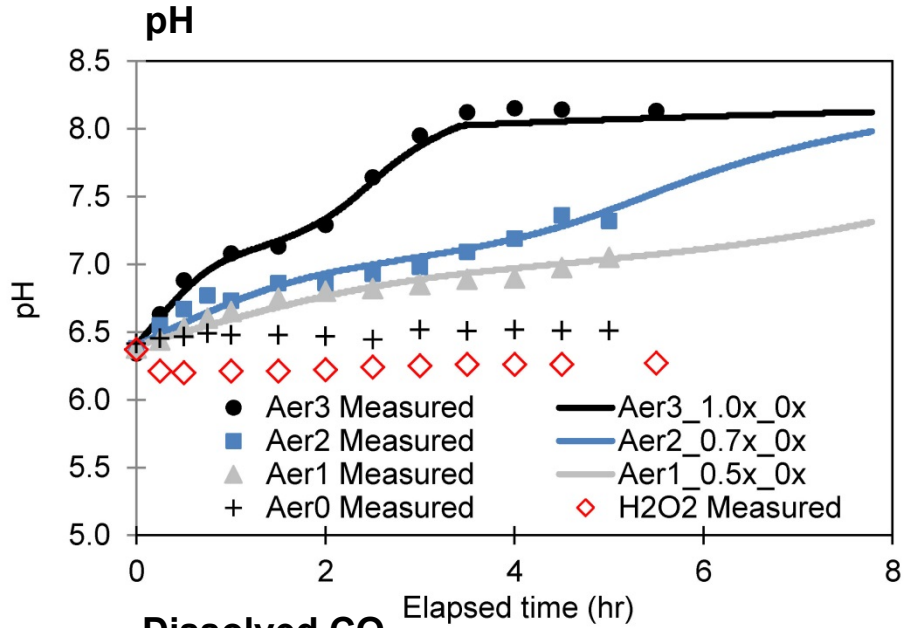
Aerated



H_2O_2 Addition

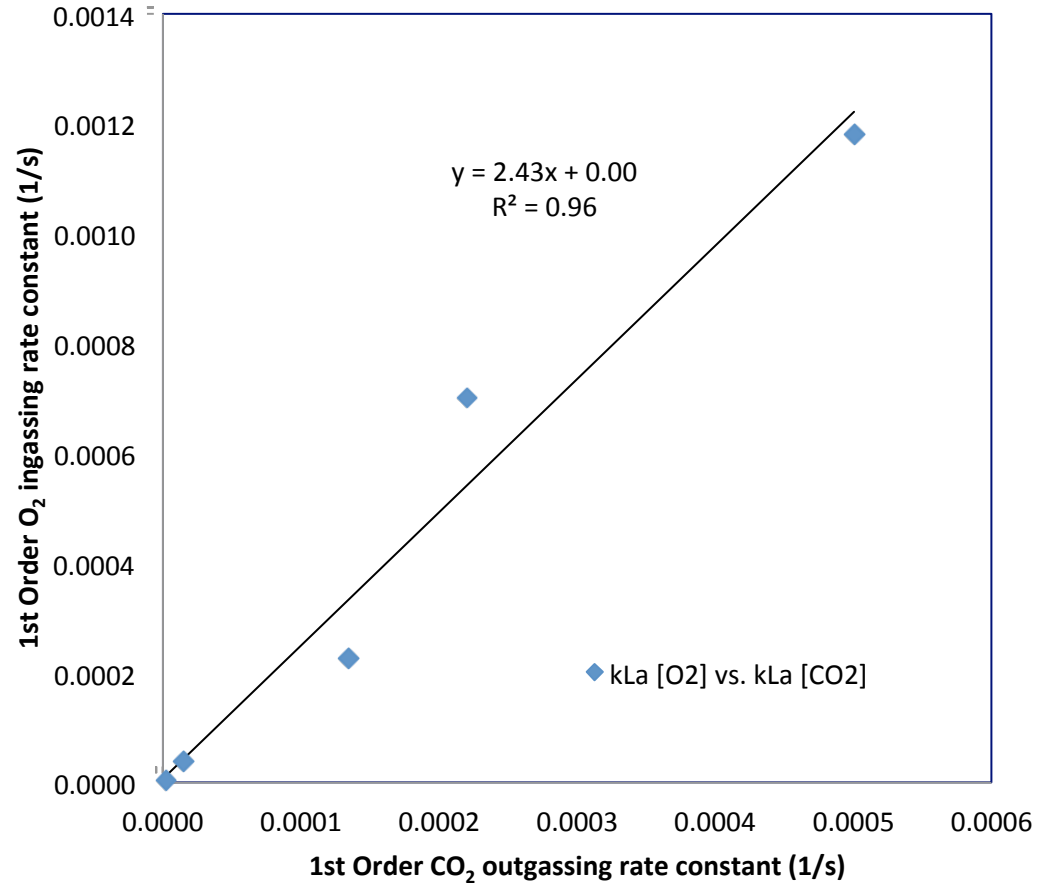
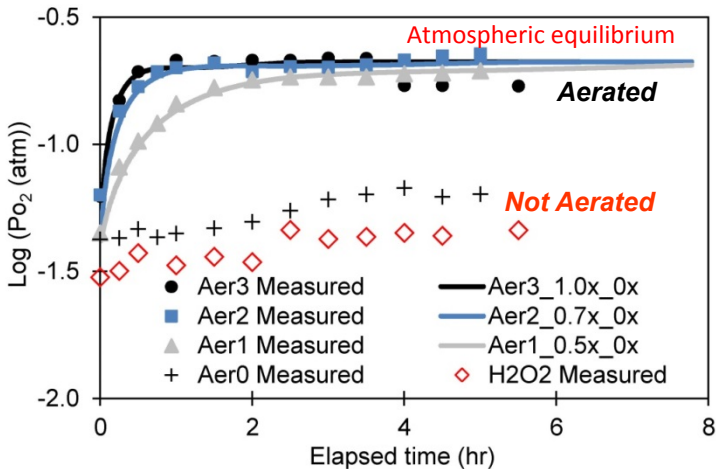
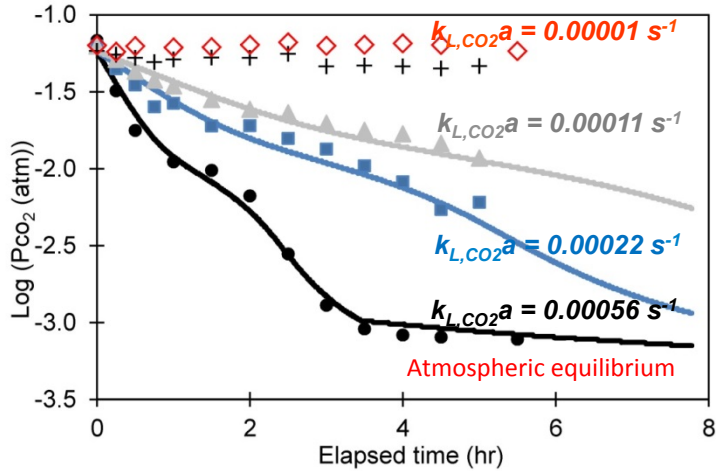


PHREEQC Coupled Kinetic Model of CO₂ Outgassing & Homogeneous Fe(II) Oxidation—Oak Hill Boreholes



CO₂ Outgassing is Proportional to O₂ Ingassing (model specifies first-order rates for out/in gassing)

$-d[C]/dt = k_{L,C}a \cdot ([C] - [C]_s)$ exponential, asymptotic approach to steady state



New Iron Oxidation Rate Model for "AMD Treat" (combines abiotic and microbial oxidation kinetics)

The **homogeneous oxidation rate law** (Stumm and Lee, 1961; Stumm and Morgan, 1996), expressed in terms of $[O_2]$ and $\{H^+\}$ ($=10^{-pH}$), describes the abiotic oxidation of dissolved Fe(II):

$$-d[Fe(II)]/dt = k_1 \cdot [Fe(II)] \cdot [O_2] \cdot \{H^+\}^{-2}$$

The **heterogeneous oxidation rate law** describes the catalytic abiotic oxidation of sorbed Fe(II) on precipitated Fe(III) oxyhydroxide surfaces, where (Fe(III)) is the Fe(III) oxyhydroxide concentration expressed as Fe in mg/L (Dempsey et al., 2001; Dietz and Dempsey, 2002):

$$-d[Fe(II)]/dt = k_2 (Fe(III)) \cdot [Fe(II)] \cdot [O_2] \cdot \{H^+\}^{-1}$$

The **microbial oxidation rate law** describes the catalytic biological oxidation of Fe(II) by acidophilic microbes, which become relevant at $pH < 5$ (Pesic et al., 1989; Kirby et al., 1999):

$$-d[Fe(II)]/dt = k_{bio} \cdot C_{bact} \cdot [Fe(II)] \cdot [O_2] \cdot \{H^+\}$$

where k_{bio} is the rate constant in $L^3/mg/mol^2/s$, C_{bact} is the concentration of iron-oxidizing bacteria in mg/L (dry weight), $[]$ indicates aqueous concentration in mol/L.

New Iron Oxidation Rate Model for "AMDTreat"— PHREEQC Coupled Kinetic Models of CO₂ Outgassing & Fe(II) Oxidation

Form1

FlowGPM 100

Fe 19.7

Estimate Fe2

Fe2 19.7

Al 0.047

Mn 3.6

pH 6.4

Alk 150

Estimate TIC

TIC 0

SO4 400

Cl 7.9

Ca 79

Mg 64

Na 5.0

TempC 15.1

SC.uS/cm 1280

DO 0.1

Duration of aeration (time for reaction)
TimeSecs : 28800 is 8 hrs

FeIIoxidation TimeSecs 28800

kLaCO2 0.0006 CO₂ outgassing rate in sec⁻¹

factr.kCO2 1 Adjustment CO₂ outgassing rate

factr.kO2 2 Adjustment O₂ ingassing rate (x kLaCO2)

factr.k1Fe 1 Adjustment abiotic homogeneous rate

factr.k2Fe 0 Adjustment abiotic heterogeneous rate

bactMPN 5.30E+11 Iron oxidizing bacteria, microbial rate

SlccPPT 0.3 Calcite saturation limit

H2O2mmol 0 Hydrogen peroxide added*

factr.kh2o2 1 Adjustment to H2O2 rate

FeIIIRecirculated FeIII 2000
Option to specify FeIII recirculation

Generate Kinetics Output

Plot Dis. Metals Plot Ca, Acidity Plot Sat Index

Kinetic variables can be adjusted, including CO₂ outgassing and O₂ ingassing rates plus abiotic and microbial FeII oxidation rates. Constants are temperature corrected.



Fell.exe

Aer3: $k_{L,CO_2}a = 0.00056 \text{ s}^{-1}$
Aer2: $k_{L,CO_2}a = 0.00022 \text{ s}^{-1}$
Aer1: $k_{L,CO_2}a = 0.00011 \text{ s}^{-1}$
Aer0: $k_{L,CO_2}a = 0.00001 \text{ s}^{-1}$

User may estimate Fe2 from Fe and pH plus TIC from alkalinity and pH. And specify H₂O₂ or recirculation of FeIII. Output includes pH, solutes, net acidity, TDS, SC, and precipitated solids.

*multiply Fe.mg by 0.0090 to get [H2O2]

Estimated CO₂ Outgassing & O₂ Ingassing Rate Constants for Various Treatment Technologies

Table S.4 Values of rate constants for CO₂ outgassing and O₂ ingassing used for kinetic models

Site	Temperature (°C)	CO ₂ Outgas			O ₂ Ingas			
		k _{L,CO2a} (s ⁻¹)	log(s ⁻¹)	log(min ⁻¹)	k _{L,O2a} (s ⁻¹)	log(s ⁻¹)	log(min ⁻¹)	
Treatment Systems								
Maelstrom (Sykesville, Trent, St.Michaels)	20	0.03	Fast	-1.52	0.26	0.06	-1.22	0.56
Surface Aerator (Renton, Rushton)	20	0.001		-3.00	-1.22	0.002	-2.70	-0.92
Mechanical Aerator (Lancashire)	20	0.0006		-3.22	-1.44	0.0012	-2.92	-1.14
Aeration Cascade/Level Spreader (Silver Cr)	20	0.01		-2.00	-0.22	0.02	-1.70	0.08
Rip-rap Spillway/Ditch (Silver Cr, Pine Forest,	20	0.005		-2.30	-0.52	0.01	-2.00	-0.22
Pond (Silver Cr, Pine Forest, Lion Mining, Flight93)	20	0.00001	Slow	-5.00	-3.22	0.00002	-4.70	-2.92
Wetland (Silver Cr, Pine Forest, Lion Mining)	20	0.00001		-5.00	-3.22	0.00002	-4.70	-2.92
Oak Hill Aeration Expts.								
Aer3	20	0.0005625	Fast	-3.25	-1.47	0.001125	-2.95	-1.17
Aer2	20	0.0002475		-3.61	-1.83	0.000495	-3.31	-1.53
Aer1	20	0.0001508		-3.82	-2.04	0.000302	-3.52	-1.74
Aer0	20	0.0000169	Slow	-4.77	-2.99	3.38E-05	-4.47	-2.69

*Gas mass-transfer rate corrected to 20°C per Rathbun (1998, Eq. 56) using the expression:

$$k_{L,a_20} = k_{L,a_TC} / (1.0241^{(TC-20)}).$$

$$k_{L,a_TC} = k_{L,a_20} * (1.0241^{(TC-20)}).$$

$k_{L,a_20} = (\text{LN}((C_1 - C_s) / (C_2 - C_s)) / t) / (1.0241^{(\text{TEMP}_{PC} - 20)})$, where C is CO₂ or O₂.

Dissolved O₂, temperature, and pH were measured using submersible electrodes.

Dissolved CO₂ was computed from alkalinity, pH, and temperature data.

Revised AMDTreat Chemical Cost Module – Caustic Titration with Pre-Aeration (Decarbonation) PHREEQC Coupled Kinetic Models of CO₂ Outgassing & Fe(II) Oxidation

The screenshot shows the PHREEQC Test window with the following settings:

- FlowGPM: 7600
- Fe: 136
- Estimate Fe2
- Fe2: 136
- Al: 0.35
- Mn: 4.1
- pH: 5.72
- Alk: 62.8
- Estimate TIC
- TIC: 62
- SO4: 1100
- Cl: 38.7
- Ca: 212
- Mg: 85.2
- Na: 25.5
- TempC: 15.4
- SC.uS/cm: 1879
- DO: 0.01
- Caustic Chemical Treatment Type:
 - Hydrated Lime
 - Pebble Quick Lime
 - Caustic Soda
- Not Aerated
- Pre-Aerated
 - TimeSecs: 76.2
 - kLaCO2: 0.03
 - factr.kCO2: 1
 - factr.kO2: 2
 - H2O2mmol: 0
 - factr.kh2o2: 0
 - SlccPPT: 0.3
- Buttons: Generate Output, Plot Dis. Conc. (checked), Plot Sat Index (unchecked)

Original option for no aeration, plus new option for **kinetic pre-aeration** (w/ wo hydrogen peroxide) that replaces original equilibrium aeration.



Dropdown kLa

PHREEQTitation_StMichaels.exe

Duration of pre-aeration in sec
CO₂ outgassing rate constant in sec⁻¹
Adjustment CO₂ outgassing rate (x kLaCO₂)
Adjustment O₂ ingassing rate (x kLaCO₂)
Hydrogen peroxide added*
Adjustment to H₂O₂ rate
Calcite saturation limit

Allows selection and evaluation of key variables that affect chemical usage efficiency.

*multiply Fe.mg by 0.0090 to get [H2O2]

New Module For AMDTreat – PHREEQC Coupled Kinetic Models of CO₂ Outgassing & Fe(II) Oxidation, with Caustic Pre-Treatment

Option to adjust initial pH with caustic

FlowGPM 8750

Fe 16.0

Estimate Fe2

Fe2 16.0

Al 0.010

Mn 6.2

pH 6.1

Alk 107

Estimate TIC

TIC 0

SO4 560

Cl 9.4

Ca 120

Mg 65

Na 13.0

TempC 14.5

SC.uS/cm 1200

DO 0.1

Add Chemical to Fix pH 7.2

Hydrated Lime

Pebble Quick Lime

Caustic Soda

FeIIoxidation TimeSecs 72000

kLaCO2 0.00001 CO₂ outgassing rate

factr.kCO2 1 Adjustment CO₂ outgassing rate

factr.kO2 2 Adjustment O₂ ingassing rate (x kLaCO2)

factr.k1Fe 1 Adjustment abiotic homogeneous rate

factr.k2Fe 1 Adjustment abiotic heterogeneous rate

bactMPN 5.3E+11 Iron oxidizing bacteria

SlccPPT 0.3 Calcite saturation limit

H2O2mmol 0 Hydrogen peroxide added

factr.kh2o2 1 Adjustment to H2O2 rate

FeIIIRecirculated FeIII 2000

Option to specify FeIII recirculation

Generate Kinetics Output

Plot Dis. Metals Plot Ca, Acidity Plot Sat Index

Variable CO₂ outgassing and O₂ ingassing rates apply. Can choose to adjust initial pH with caustic. The required quantity of caustic is reported in units used by AMDTreat.

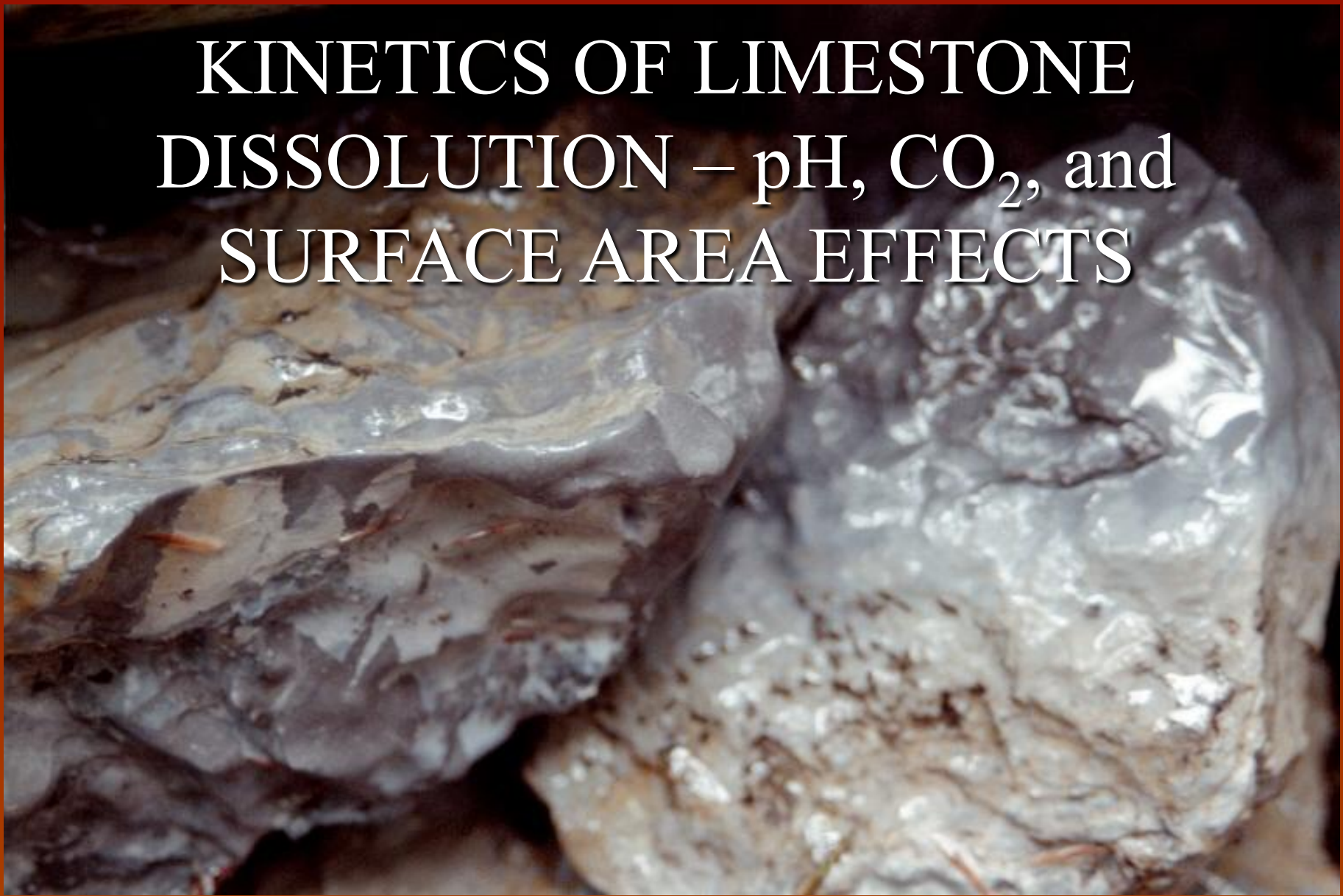


Caustic+FeII.exe

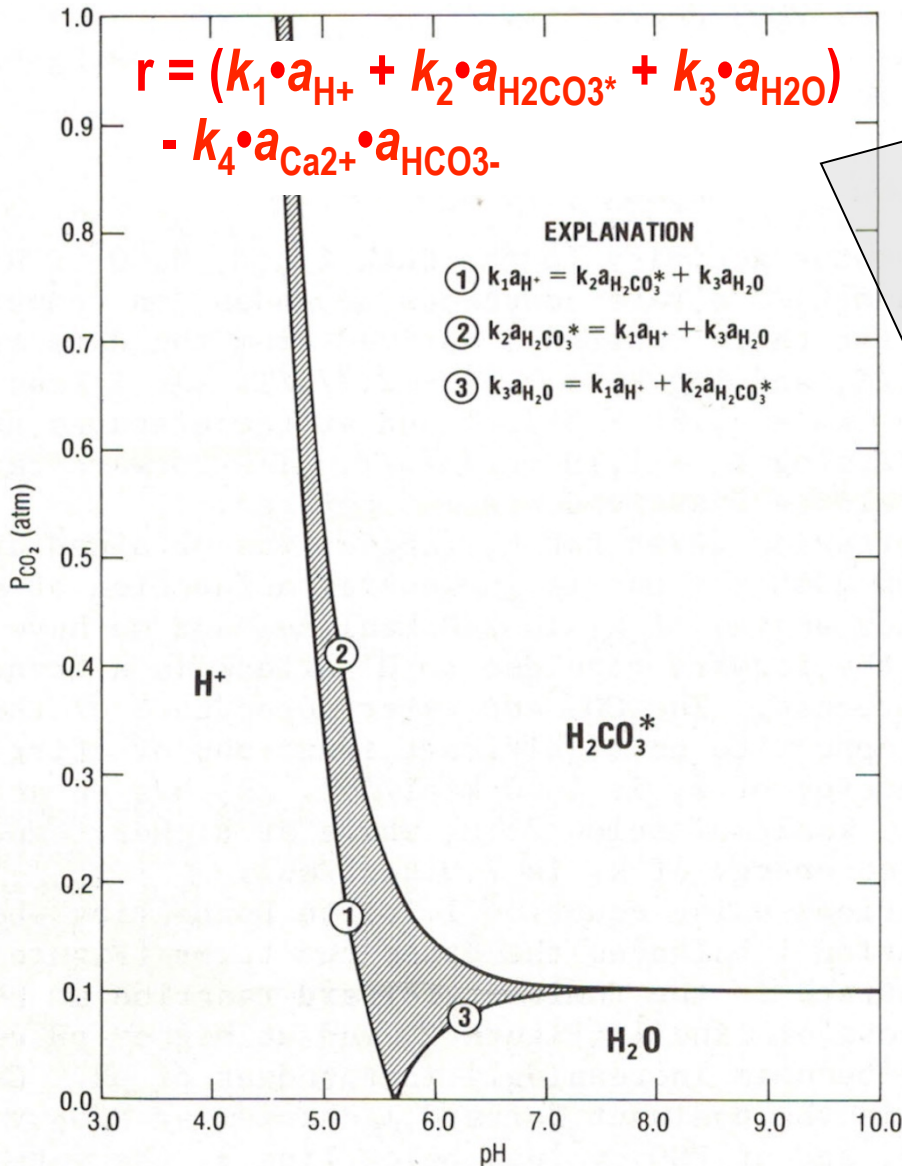
Kinetic variables, including CO₂ outgassing and O₂ ingassing rates plus abiotic and microbial FeII oxidation rates, can be adjusted by user. In addition to caustic chemicals, hydrogen peroxide and recirculation of FeIII solids can be simulated.

*multiply Fe.mg by 0.0090 to get [H2O2]

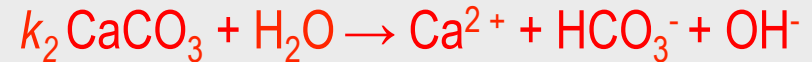
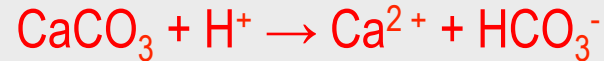
KINETICS OF LIMESTONE DISSOLUTION – pH, CO₂, and SURFACE AREA EFFECTS



Limestone Dissolution Rate Model for AMD Treat ("PWP" model emphasizes pH and CO₂)



According to Plummer, Wigley, and Parkhurst (1978), the rate of CaCO₃ dissolution is a function of three forward (dissolution) reactions:



k_4

Although H⁺, H₂CO₃^{*}, and H₂O reaction with calcite occur simultaneously, the forward rate is dominated by a single species in the fields shown. More than one species contributes significantly to the forward rate in the gray stippled area. Along the lines labeled 1, 2, and 3, the forward rate attributable to one species balances that of the other two.

Limestone Dissolution Rate Model for AMD Treat (generalized expression corrects for surface area)

Appelo and Postma (2005) give a generalized rate expression for calcite dissolution that considers physical characteristics of the system as well as solution chemistry:

$$R = k \cdot (A/V) \cdot (1 - \Omega)^n$$

where A is calcite surface area, V is volume of solution, Ω is saturation state ($IAP/K = 10^{SI_{cc}}$), and k and n are empirical coefficients that are obtained by fitting observed rates.

For the “PWP” model applied to 1 liter solution, the overall rate becomes:

$$R = (k_1 \cdot a_{H^+} + k_2 \cdot a_{H_2CO_3^*} + k_3 \cdot a_{H_2O}) \cdot (A) \cdot (1 - 10^{(n \cdot SI_{cc})})$$

Plummer and others (1978) reported the forward rate constants as a function of temperature (T , in K), in millimoles calcite per centimeter squared per second ($mmol/cm^2/s$):

$$\log k_1 = 0.198 - 444 / T$$

$$\log k_2 = 2.84 - 2177 / T$$

$$\log k_3 = -5.86 - 317 / T \text{ for } T \leq 298; \log k_3 = -1.10 - 1737 / T \text{ for } T > 298$$

Limestone Dissolution Rate Model for AMDTreat (surface area correction for coarse aggregate)

Surface area for various coarse aggregates (bold indicates sizes commonly used in limestone beds; 2NS used in cubitainers).

Gradation Number		Weight (g) Average Particle	Particle Dimensions (cm)				Particle Surface Area (cm ²)			Unit Surface Area (cm ² /g)		
AASHTO	PA		Long Axis	Inter-mediate	Short Axis	Average Axis	Rectan-gular Prism	Sphere	Ellipsoid	Rectan-gular Prism	Sphere	Ellipsoid
R-5		22160.145	45.72	22.86	13.34	27.31	3919.35	2342.26	2862.08	0.18	0.11	0.13
R-4		7113.133	30.48	16.51	8.89	18.63	1841.93	1089.98	1319.11	0.26	0.15	0.19
R-3		1185.522	16.51	8.89	5.08	10.16	551.61	324.29	395.61	0.47	0.27	0.33
1	4	341.978	8.89	6.35	3.81	6.35	229.03	126.68	155.24	0.67	0.37	0.45
3	3A	78.166	5.08	3.81	2.54	3.81	83.87	45.60	56.39	1.07	0.58	0.72
5		9.771	2.54	1.91	1.27	1.91	20.97	11.40	14.10	2.15	1.17	1.44
57	2B	3.257	2.54	1.27	0.635	1.48	11.29	6.90	8.25	3.47	2.12	2.53
	2NS	9.771	2.54	1.91	1.27	1.91	20.97	11.40	14.10	2.15	1.17	1.44
67	2	1.832	1.91	0.95	0.635	1.16	7.26	4.26	5.28	3.96	2.32	2.88
	1NS	1.221	1.27	0.95	0.635	0.95	5.24	2.85	3.52	4.29	2.33	2.89
7		1.221	1.27	0.95	0.635	0.95	5.24	2.85	3.52	4.29	2.33	2.89
8		0.382	0.95	0.79	0.3175	0.69	2.62	1.49	1.70	6.87	3.90	4.44
	1B	0.382	0.95	0.79	0.3175	0.69	2.62	1.49	1.70	6.87	3.90	4.44



Particle dimensions were estimated on the basis of ranges for graded materials reported in Pennsylvania Department of Environmental Protection, 2000, Erosion and sediment pollution control program manual: Harrisburg, Pennsylvania Dept. Environmental Protection Bureau of Watershed Management, Document No. 363-2134-008, 180 p. (tables 9 and 10A).

Plummer, Wigley, and Parkhurst (1978) reported unit surface area (SA) of 44.5 and 96.5 cm²/g for “coarse” and “fine” particles, respectively, used for empirical testing and development of PWP rate model. These SA values are 100 times larger than those for typical limestone aggregate. Multiply cm²/g by 100 g/mol to get surface area (A) units of cm²/mol used in AMDTreat rate model.

Surface area computed for various geometric forms:

Sphere: $4\pi(\text{Average of Axes}/2)^2$

Rectangular Prism: $2(\text{Long Axis} \times \text{Short Axis}) + 2(\text{Long Axis} \times \text{Intermediate Axis}) + 2(\text{Short Axis} \times \text{Intermediate Axis})$

Ellipsoid: $(\pi \times D^2)/S$, where $D = 2(\text{vol}/(4/3\pi))^{1/3}$ $S = 1.15 - 0.25E$ $E = \text{Long Axis}/D$

Volume computed for same geometric forms:

Sphere: $4/3\pi(\text{Average Axis}/2)^3$

Rectangular Prism: $(\text{Long Axis} \times \text{Short Axis} \times \text{Intermediate Axis})$

Ellipsoid: $4/3\pi(\text{Long Axis}/2 \times \text{Short Axis}/2 \times \text{Intermediate Axis}/2)$

For ellipsoid sphere, this reduces to $0.5236 \times \text{Long Axis} \times \text{Short Axis} \times \text{Intermediate Axis}$

Santomartino and Webb (2007, AG, 22:2344–2361) estimated volume of ellipsoid as $0.6 \times \text{volume of rectangular prism of same dimensions}$.

New Module For AMDTreat – PHREEQC Kinetic Model of Limestone Dissolution

Form1

TimeSecs : 7200 is 2 hrs

FlowGPM 690

LimestoneDiss TimeSecs 7200

Fe 14.0

SAcc 44.5e+02 Surface area, cm²/mol **

Estimate Fe2

EXPcc 0.67 Equilibrium approach

Fe2 14.0

M/M0cc 1.00 Mass available

Al 0.09

Mn 3.1

pH 5.79

Alk 26

Estimate TIC

TIC 42.25

SO4 330

Cl 4.0

Ca 56

Mg 51

Na 7.4

TempC 11.63

SC.uS/cm 700

DO 0.4

Generate Kinetics Output

Plot Dis. Metals Plot Ca, Acidity Plot Sat Index

**Multiply surface area (SA) in cm²/g by 100 to get SAcc in cm²/mol.

Calcite dissolution rate model of Plummer, Wigley, and Parkhurst (PWP; 1978). Empirical testing and development of PWP rate model based on “coarse” and “fine” calcite particles with surface areas of 44.5 and 96.5 cm²/g, respectively.



Limestone.PWP.exe

Surface area and exponential corrections permit application to larger particle sizes (0.45 to 1.44 cm²/g) used in treatment systems.

New Module For AMDTreat — PHREEQC Coupled Kinetic Models of Limestone Dissolution & Fe(II) Oxidation

The screenshot shows a software window titled 'Form1' with the following parameters and controls:

- FlowGPM: 690
- Fe: 14.0
- Estimate Fe2
- Fe2: 14.0
- Al: 0.09
- Mn: 3.1
- pH: 5.79
- Alk: 26
- Estimate TIC
- TIC: 42.25
- SO4: 330
- Cl: 4.0
- Ca: 56
- Mg: 51
- Na: 7.4
- TempC: 11.63
- SC.uS/cm: 700
- DO: 0.4
- LimestoneDiss TimeSecs: 14240
- SAccDIS: 0.72e+02 Surface area
- EXPccDIS: 0.67 Equilibrium approach
- M/M0cc: 1.00 Mass available
- FeIIoxidation TimeSecs: 47015
- Use LimestoneDiss Effluent
- kLaCO2: 0.00005 CO₂ outgassing rate
- factr.kCO2: 1 Adjustment CO₂ outgassing rate
- factr.kO2: 2 Adjustment O₂ ingassing rate (x kLaCO2)
- factr.k1Fe: 1 Adjustment abiotic homogeneous rate
- factr.k2Fe: 0 Adjustment abiotic heterogeneous rate
- bactMPN: 5.30E+11 Iron oxidizing bacteria
- SlccPPT: 0.3 Calcite saturation limit
- H2O2mmol: 0 Hydrogen peroxide added
- factr.kh2o2: 1 Adjustment to H2O2 rate
- FeIIIRecirculated FeIII: 2000
- Generate Kinetics Output
- Plot Dis. Metals Plot Ca, Acidity Plot Sat Index

Rate models for calcite dissolution, CO₂ outgassing and O₂ ingassing, and FeII oxidation are combined to evaluate possible reactions in passive treatment systems.



Limestone+FeII.exe

Can simulate limestone treatment followed by gas exchange and FeII oxidation in an aerobic pond or aerobic wetland, or the independent treatment steps (not in sequence).

PHREEQC Coupled Kinetic Models Sequential Steps

Limestone Dissolution + Fe(II) Oxidation

Pine Forest ALD + Aerobic Wetlands

FormSequential

FlowGPM 690

Fe 14.0

Estimate Fe2

Fe2 14.0

Al 0.09

Mn 3.1

pH 5.79

Alk 26

FeIII Recirculated?

Estimate TIC

Limestone and FeII Kinetic Constants

EXPccDIS 0.67 M/M0cc 1.00

factr.kCO2 1 factr.kO2 2

factr.k1Fe 1 factr.k2Fe 0

bactMPN 5.3E+11 SlccPPT 0.3

H2O2mmol 0 factr.kh2o2 1

	Step	Time(s)	kLaCO2(1/s)	SAcc(cm2/mol)	Temp2(C)	FeIII(mg)
TIC	1:	14240	0.00001	0.72e+02	11.63	0
SO4	2:	60	0.02	0	11.6	0
Cl	3:	47015	0.00002	0	12.16	5
Ca	4:	15	0.001	0	12.16	0
Mg	5:	28814	0.00003	0	12.15	3
Na	6:	15	0.02	0	12.15	0
TempC	7:	21972	0.00002	0	12.04	0
SC.uS/cm	8:	15	0.02	0	12.04	0
TDS	9:	3979	0.00002	0	11.88	0

DO 0.4

Plot Dis. Metals Plot Ca, Acidity Plot Sat Index

Generate Sequential Kinetics Output

Sequential steps: Variable detention times, adjustable CO₂ outgassing rates, limestone surface area, temperature, and FeII.



Next slide

Limestone+FeIIseq.exe

Can simulate passive treatment by anoxic or oxic limestone bed, open (limestone) channels or spillways, aerobic cascades, ponds, and wetlands.

PHREEQC Coupled Kinetic Models Sequential Steps— Pine Forest ALD + Aerobic Wetlands



Step	Treatment
1	ALD
2	Riprap
3	Pond
4	Cascade
5	Wetland
6	Cascade
7	Wetland
8	Cascade
9	Wetland



Limestone+Fellseq_PineFor151212.exe



LS+Fellseq_kinetics.sel - Shortcut.lnk



PineForest_Field_151212t.xlsx - Shortcut.lnk

PHREEQC Coupled Kinetic Models Sequential Steps Caustic + Limestone Dissolution + Fe(II) Oxidation Silver Creek Aerobic Wetlands

FormSequential

FlowGPM 750

Fe 20.0

Estimate Fe2

Fe2 20.0

Al 0.19

Mn 2.95

pH 6.01

Alk 45.5

Estimate TIC

TIC 29.8

SO4 150

Cl 4.0

Ca 45.7

Mg 28.3

Na 2.6

TempC 12.12

SC.uS/cm 502

TDS 250

DO 0.1

Add Chemical to Fix Initial pH 7.3

CaO Ca(OH)2 NaOH

Limestone and FeII Kinetic Constants

EXPcc 0.67 M/M0cc 1.00

factr.kCO2 1 factr.kO2 2

factr.k1Fe 1 factr.k2Fe 0

bactMPN 5.3E+11 SlccPPT 0.3

H2O2mmol 0 factr.kh2o2 1

FeIII Recirculated?

Step	Time(s)	kLaCO2(1/s)	SAcc(cm2/mol)	Temp2(C)	FeIII(mg)
1:	4074	0.000001	0	13.91	0
2:	30	0.005	0	14.11	0
3:	493128	0.000001	0	17.93	5
4:	30	0.005	0	18.41	0
5:	842859	0.000003	0	25.23	3
6:	120	0.0075	0.72e+02	24.45	0
7:	112429	0.000005	0	25.55	0
8:	120	0.0075	0.72e+02	24.49	0
9:	141927	0.000005	0	28.97	0

Generate Sequential Kinetics Output

Plot Dis. Metals Plot Ca, Acidity Plot Sat Index

Sequential steps: Pre-treatment with caustic and/or peroxide and, for each subsequent step, variable detention times, adjustable CO₂ outgassing rates, limestone surface area, temperature, and FeII.



Next slide

Caustic+Limestone+FeIIseq.exe

Can simulate active treatment, including chemical addition or aeration, or passive treatment, including anoxic or oxic limestone bed, open (limestone) channels or spillways, aerobic cascades, ponds, and wetlands.

PHREEQC Coupled Kinetic Models Sequential Steps— Silver Creek Aerobic Wetlands



Caustic+LS+Fellseq_SilCr160808.exe



Caustic+LS+Fellseq_kinetics.sel - Shortcut.lnk



SilverCrk_Field_160808t.xlsx - Shortcut.lnk

Conclusions

- ✓ Geochemical kinetics tools using PHREEQC have been developed to evaluate mine effluent treatment options.
- ✓ Graphical and tabular output indicates the pH and solute concentrations in effluent.
- ✓ By adjusting kinetic variables or chemical dosing, various passive and/or active treatment strategies can be simulated.
- ✓ AMDTreat cost-analysis software can be used to evaluate the feasibility for installation and operation of treatments that produce the desired effluent quality.

Disclaimer / Release Plans

“Although this software program has been used by the U.S. Geological Survey (USGS), no warranty, expressed or implied, is made by the USGS or the U.S. Government as to the accuracy and functioning of the program and related program material nor shall the fact of distribution constitute any such warranty, and no responsibility is assumed by the USGS in connection therewith.”

- ✓ FY2017 Development, beta testing and review.
- ✓ FY2018 Official USGS “software release” planned:
- ✓ <https://water.usgs.gov/software/lists/geochemical>
- ✓ FY2018 Incorporation of PHREEQC treatment simulations with AMDTreat to be released by OSMRE:
- ✓ <http://amd.osmre.gov/>

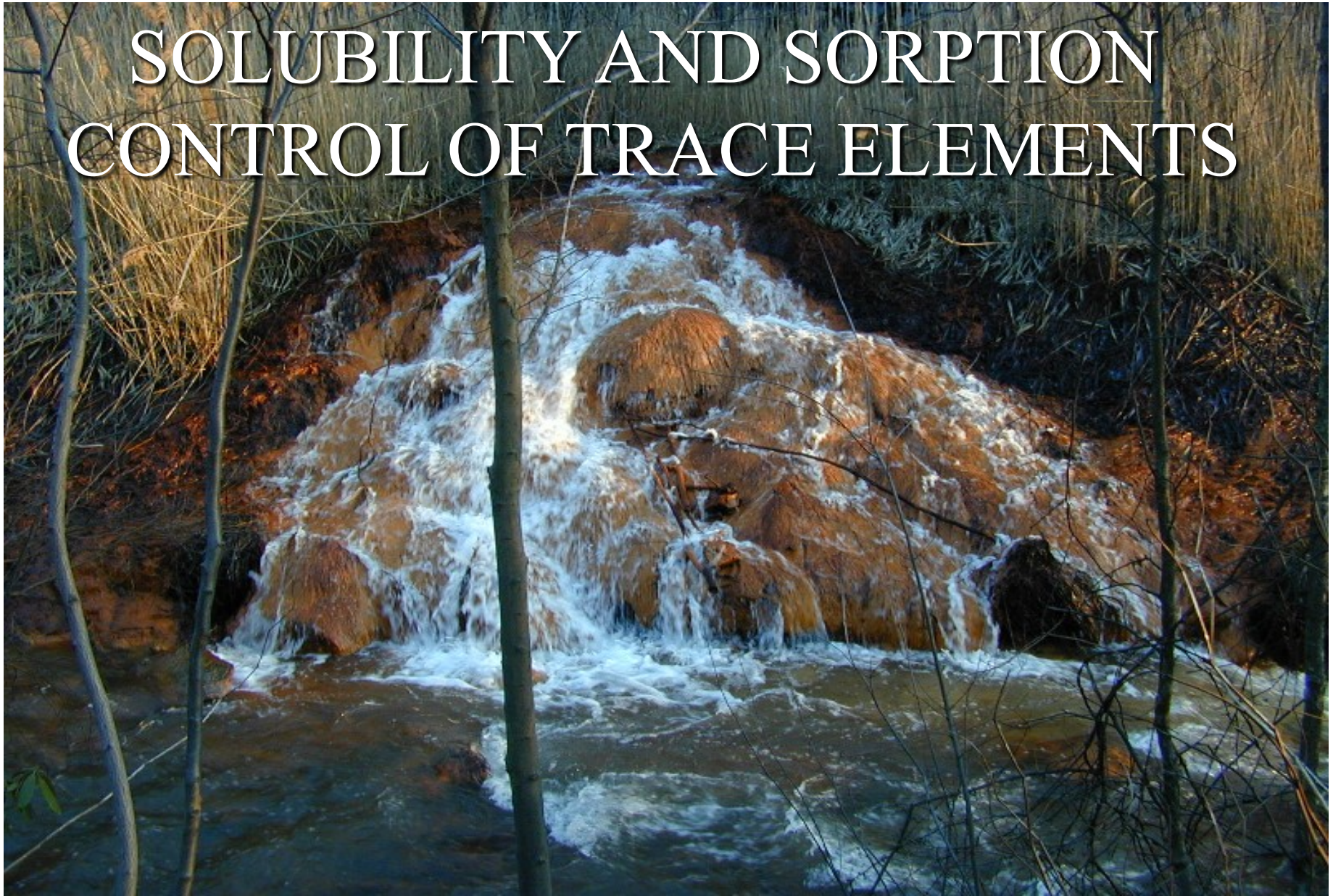
Questions?

- ✓ Are the current models capable of simulating manganese (MnII) oxidation kinetics?
- ✓ Can the models simulate the adsorption of cations by hydrous ferric oxides (HFO) as a kinetic process?
- ✓ Have you considered adsorption based rate models for the heterogeneous FeII and MnII oxidation kinetics?
- ✓ Does the limestone model consider changes in surface area of due to its dissolution or the accumulation of HFO coatings?
- ✓ Does the microbial FeII oxidation rate model consider oxidation by neutrophilic iron bacteria such as *Gallionella* or *Leptothrix*?
- ✓ What about the simulation of anaerobic processes in a BCR (Biochemical Reactor) and precipitation of metal sulfides?

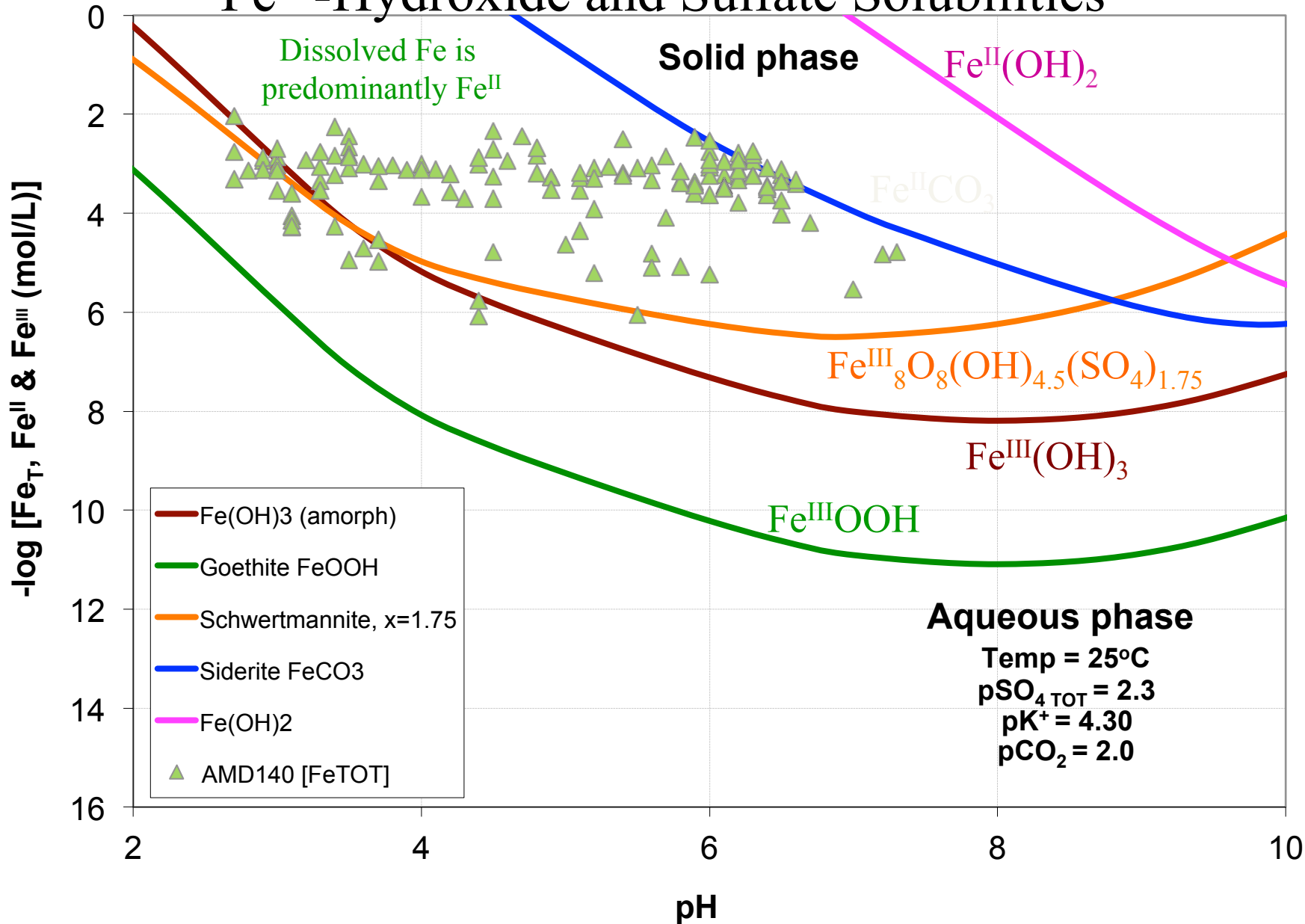
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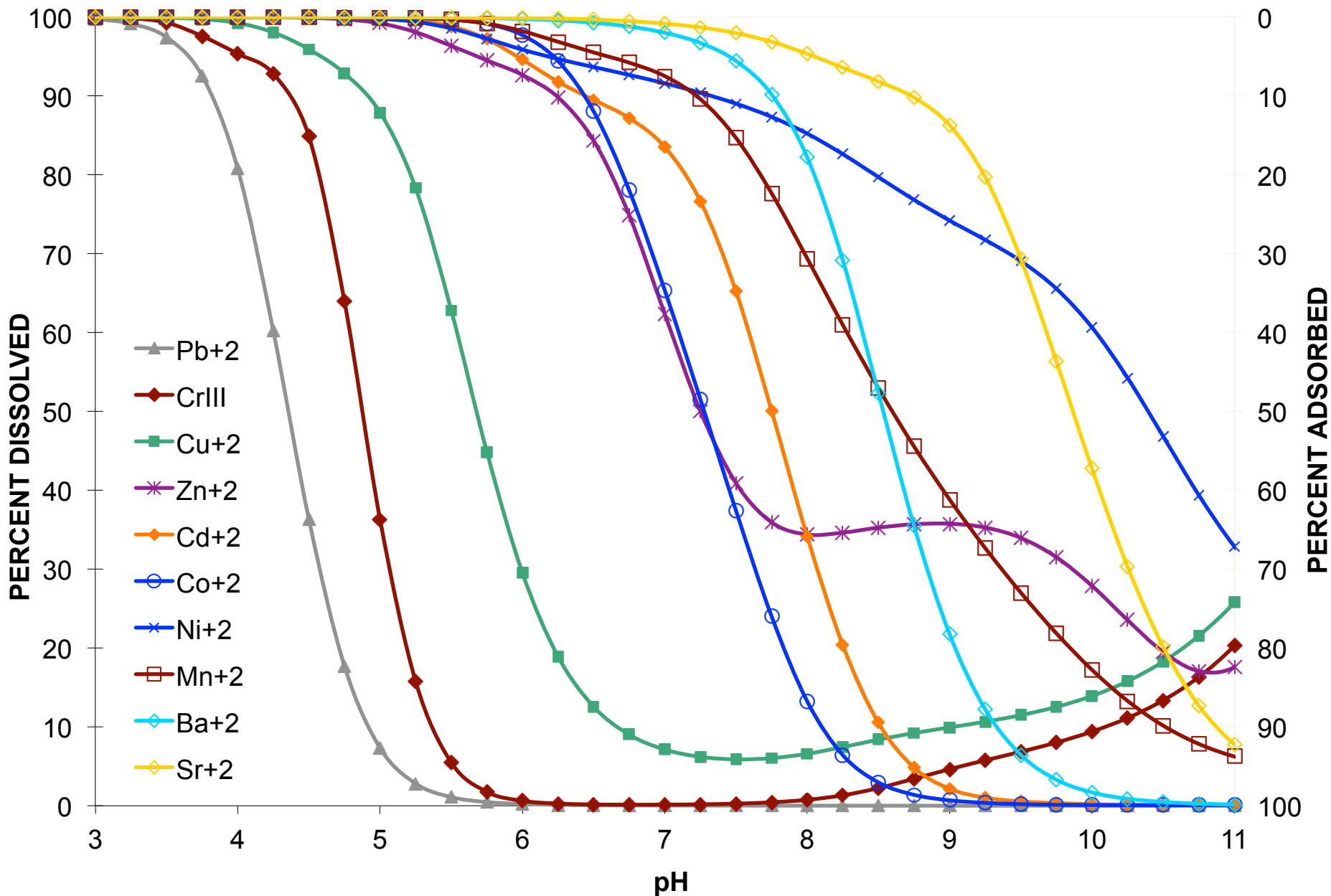
SOLUBILITY AND SORPTION CONTROL OF TRACE ELEMENTS



Fe Limited by Fe^{II}-Carbonate and Fe^{III}-Hydroxide and Sulfate Solubilities



SORPTION OF CATIONS ON "HFO"



SORPTION OF ANIONS ON "HFO"

