

Decision Support System for Matrix Diffusion Modeling

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GSI Environmental Inc.



Fall 2014 NARPM Presents Series

Acknowledgements



- Dr. Tom Sale, Colorado State
- Dr. Beth Parker, U. of Guelph
- SERDP/ESTCP
- Schlumberger, Geosyntec
- USEPA TIO



Road Map



- ◆ Introduction

- ➔ **Matrix Diffusion Background**

- ◆ Options for Modeling Matrix Diffusion
- ◆ Introduction to MDT – Square Root Model
- ◆ Dandy-Sale Model in the MDT
- ◆ Case Study 1
- ◆ Case Study 2
- ◆ Wrap-up and Open Discussion

Mini Road Map



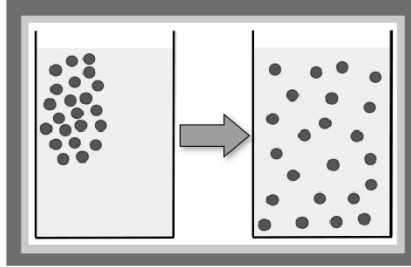
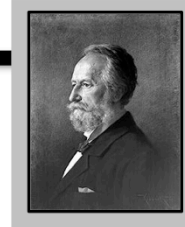
➔ Matrix Diffusion Background

- ◆ Lines of Evidence
- ◆ New Conceptual Model
- ◆ Collecting Field Samples

What is Diffusion?

Diffusion describes the spread of particles through random motion from regions of higher concentration to regions of lower concentration.

Key people: Fourier (1822), Fick (1855), Einstein (1905), Smoluchowski (1906)



$$J = D \frac{dC}{dx}$$

J = Diffusive flux flowing through a particular cross section
(mg / meter² / sec)

D = Diffusion coefficient
(meter² / sec)

$\frac{dC}{dx}$ = Concentration gradient
(mg / liter / meter)

Coffee Cup: **Convection + diffusion**

Laminar Groundwater: **Molecular diffusion - movement of molecules only**

Incomplete History of Matrix Diffusion in Groundwater

Foster (1975): Chalk system in England.

Where is the tritium going?

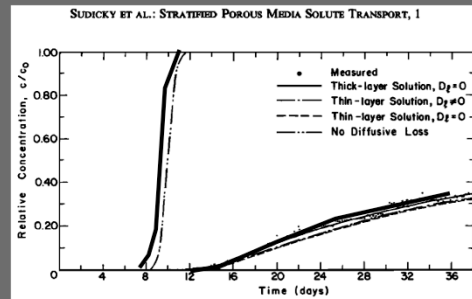
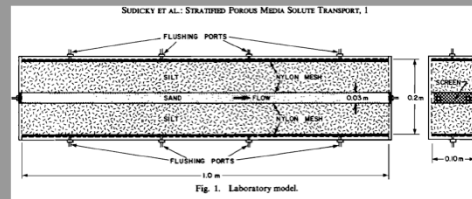
Goodall and Quigley (1977): Core analysis.

Matrix diffusion (30 cm penetration in clay) vs. advection in clay (4 cm).

Matrix Diffusion
“overwhelms” advection..

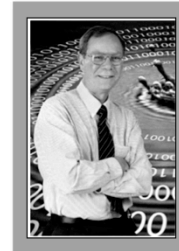


Incomplete History of Matrix Diffusion in Groundwater



Sudicky, Gillham, and Frind (WRR: 1985):

“...these effects are the result of a transient redistribution of the tracer across the strata by transverse molecular diffusion ...”

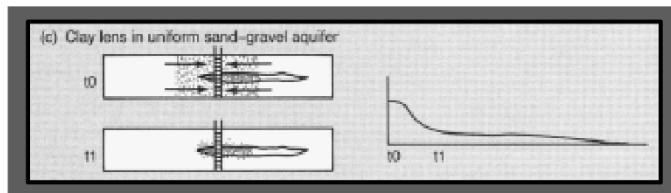


Incomplete History of Matrix Diffusion in Groundwater

Mackay and Cherry (ES&T: 1989)

“As plumes spread through aquifers, the dissolved contaminants move quickly through more permeable zones while they slowly invade the less permeable ones by flow or diffusion.”

“Over the years and decades, this invasion can cause the plume to occupy large volumes of low permeability material. To obtain clean water from wells, it is generally necessary for the lower permeability parts of the aquifer system to be cleaned as well as the high permeability zones.



Incomplete History of Matrix Diffusion in Groundwater

Parker, Gillham, Cherry (G. W.: 1994):

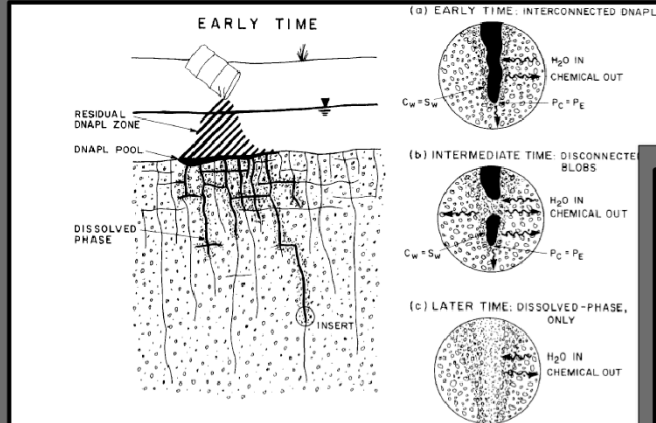


Fig. 1. Revised conceptual model for dense, immiscible organic liquid distribution at the individual fracture scale in fractured porous media: (a) Early time conditions with the DNAPL (nonwetting fluid) invading the fracture and dissolution occurring into the water film (wetting fluid) and subsequent diffusion into the adjacent porous matrix. (b) Intermediate time conditions illustrating disconnected DNAPL blobs in rough-walled fractures resulting from mass loss by diffusion into the matrix. (c) Later time conditions when all immiscible phase has dissolved and diffusion haloes exist around previous, DNAPL-filled fractures.

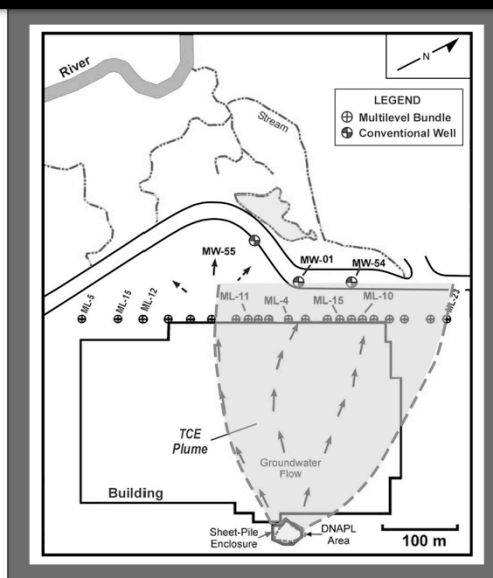


Matrix diffusion can soak up DNAPL in fractures – sometimes really quickly (days to weeks).

Incomplete History of Matrix Diffusion in Groundwater

**Chapman and Parker
(WRR: 2005).**

“Vertical back diffusion from the aquitard combined with horizontal advection and vertical transverse dispersion account for the TCE distribution in the aquifer and that the aquifer TCE will remain much above the MCL for centuries.”



Modified from figure in Chapman and Parker, 2005.

Frequently Asked Questions (Sale et al, 2008)

- Provides quick access to key concepts and references for those who need to know more
- Matrix-diffusion centric
- Tom Sale, Chuck Newell, Hans Stroo, Rob Hincsee, and Paul Johnson



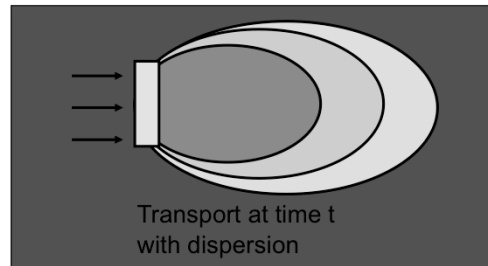
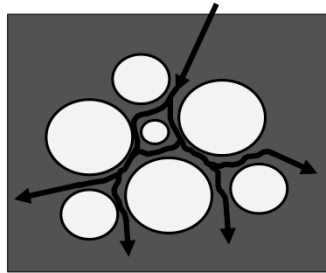
August 2008

Tom Sale, Charles Newell,
Hans Stroo, Robert Hincsee, and
Paul Johnson



Old Plume Paradigm? Advection Dispersion Model

- Advection
- Adsorption
- Dispersion
- Biodegradation



New Plume Paradigm Heterogeneity Rules, Even in “Sandy Aquifers”

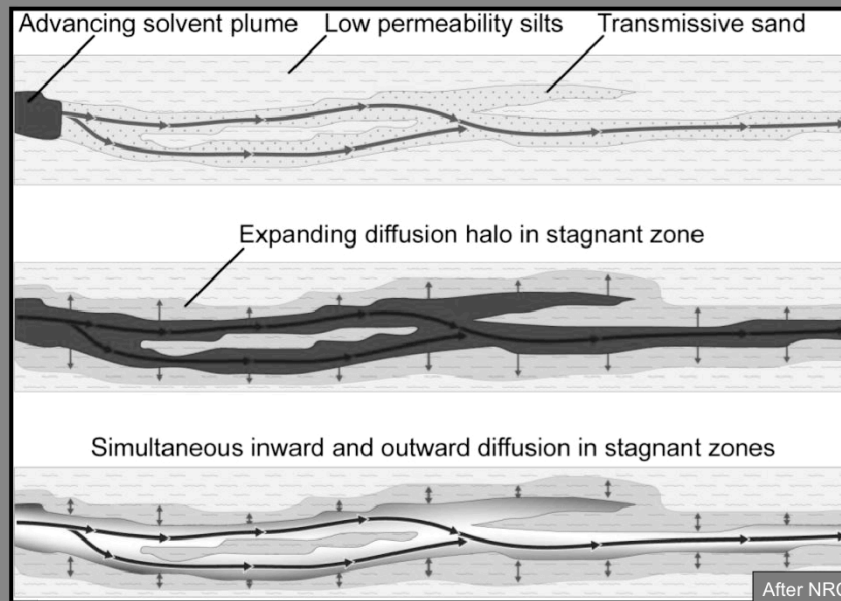


Matrix Diffusion Paradigm:
Remediation Hydraulics (CRC Press)
Fred Payne, Joseph Quinnan, Scott Potter

Image from Fred Payne /ARCADIS

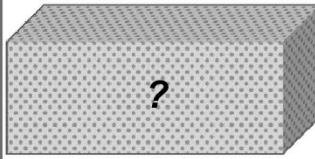
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New Plume Paradigm Matrix Diffusion

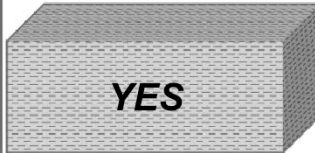


Where is Matrix Diffusion Important?

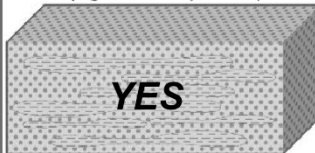
(I) Granular Media
with Mild Heterogeneity and
Moderate to High Permeability
(e.g. eolian sands)



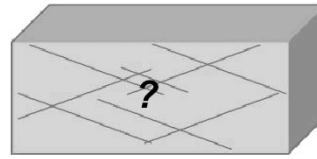
(II) Granular Media with Mild
Heterogeneity and Low Permeability
(e.g. lacustrine clay)



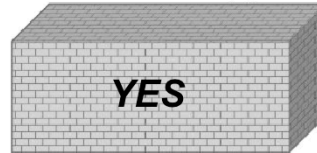
(III) Granular Media With Moderate to
High Heterogeneity
(e.g. deltaic deposition)



(IV) Fracture Media
with Low Matrix Porosity
(e.g. crystalline rock)



(V) Fracture Media
with High Matrix Porosity
(e.g. limestone, sandstone
or fractured clays)



After NRC 2005

Mini Road Map



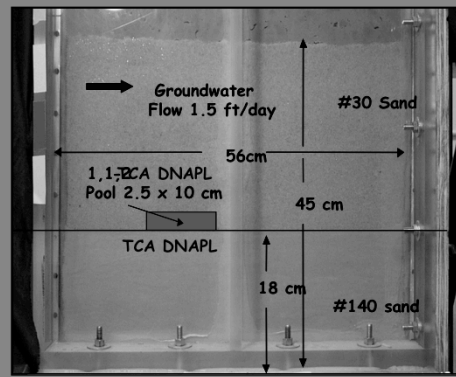
- ◆ **Matrix Diffusion Background**

- ➔ **Lines of Evidence**

- ◆ **New Conceptual Model**

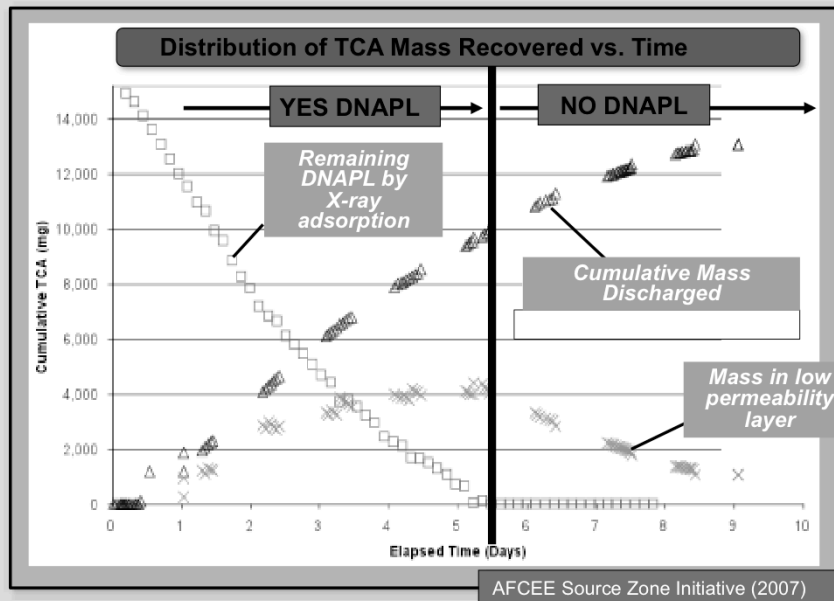
- ◆ **Collecting Field Samples**

Two layer sand tank study Colorado School of Mines (Tissa Illangasekare and Bart Wilkins)

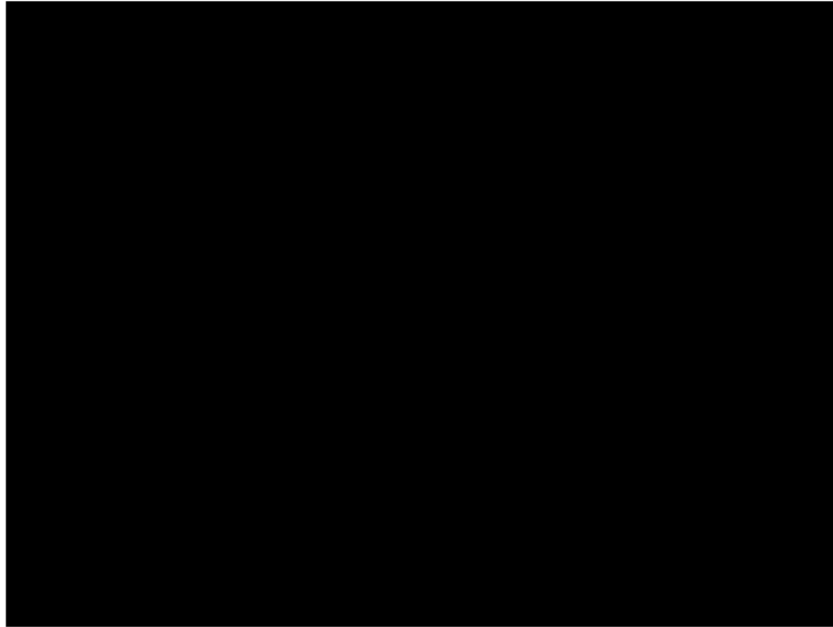


AFCEE Source Zone Initiative (2007)

Distribution of TCA Mass Recovered vs. Time

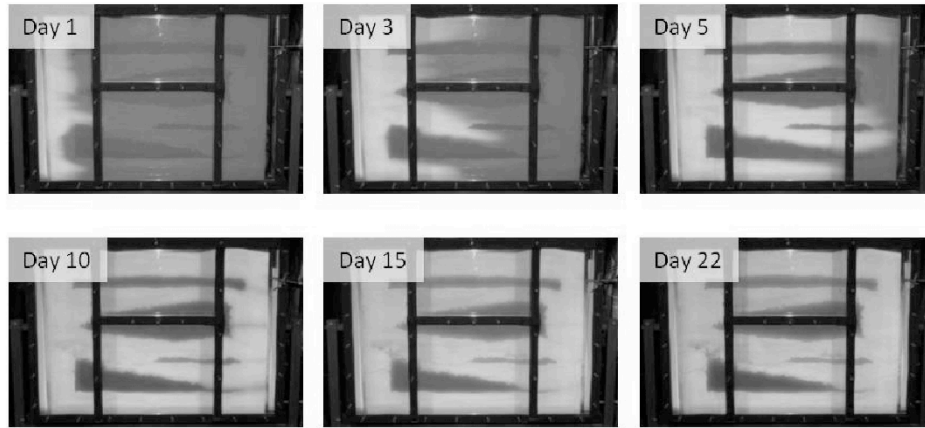


Matrix Diffusion Movie
Doner and Sale, Colorado State University



Matrix Diffusion Movie Doner and Sale, Colorado State University

Loading Phase



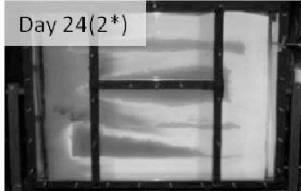
To Download: www.gsi-net.com

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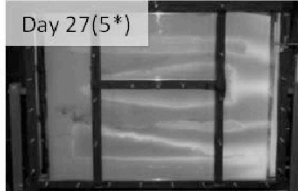
Matrix Diffusion Movie Doner and Sale, Colorado State University

Flushing Phase

Day 24(2*)



Day 27(5*)



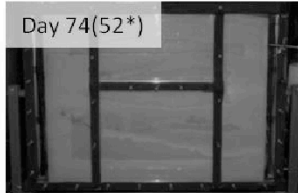
Day 31(11*)



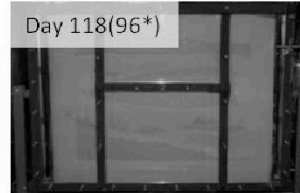
Day 42(20*)



Day 74(52*)



Day 118(96*)

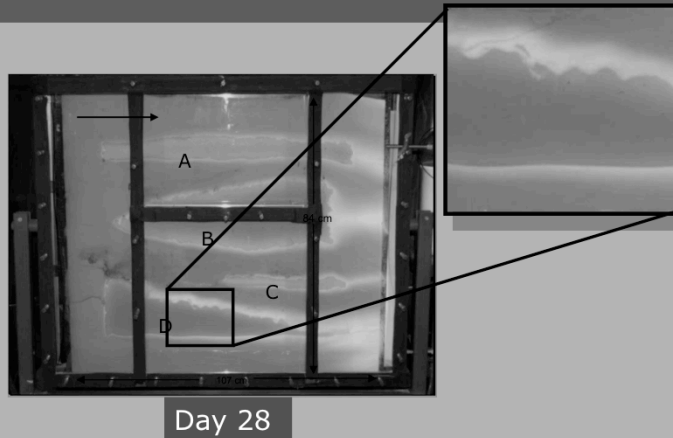


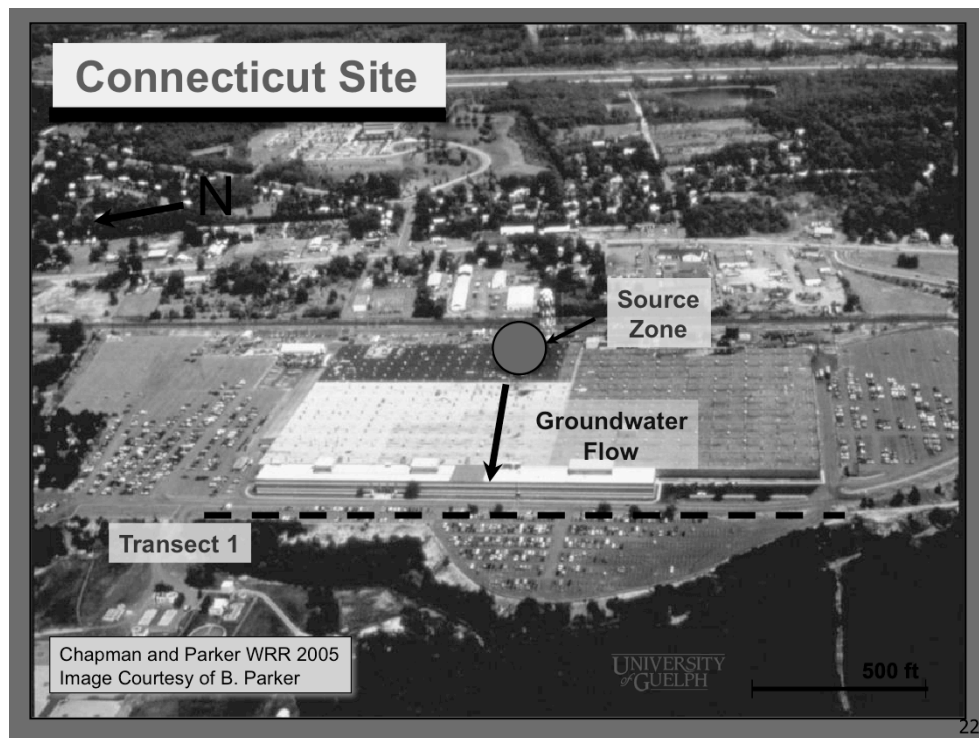
To Download: www.gsi-net.com

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Key Point – Matrix Diffusion is a Small Scale Phenomena

Matrix diffusion governed by concentrations gradients that occur at scales of *centimeters to millimeters*.

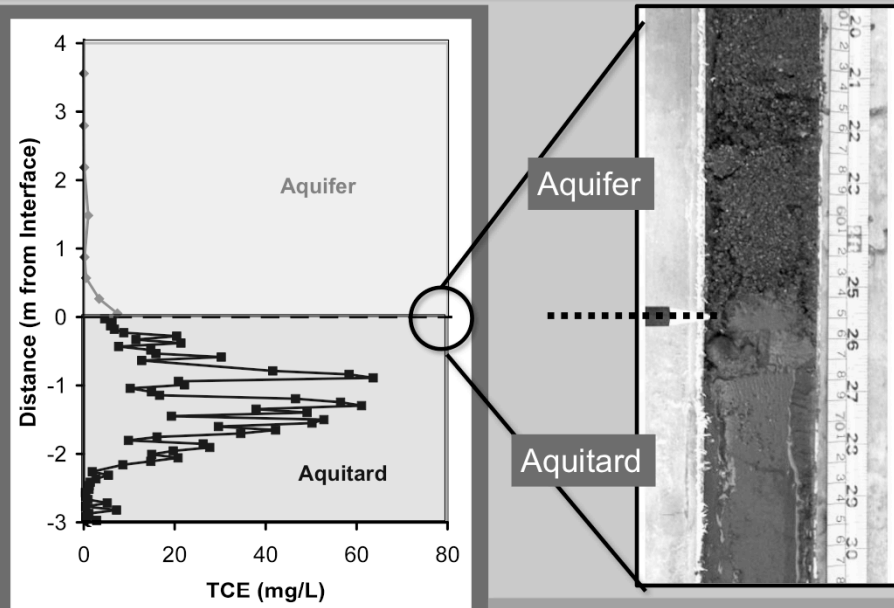




Aerial photograph – source area east of facility, monitoring transect along west side of facility 900 ft from source along entire width of facility (~1400 ft).

High-Resolution Data from Core

UNIVERSITY
of GUELPH



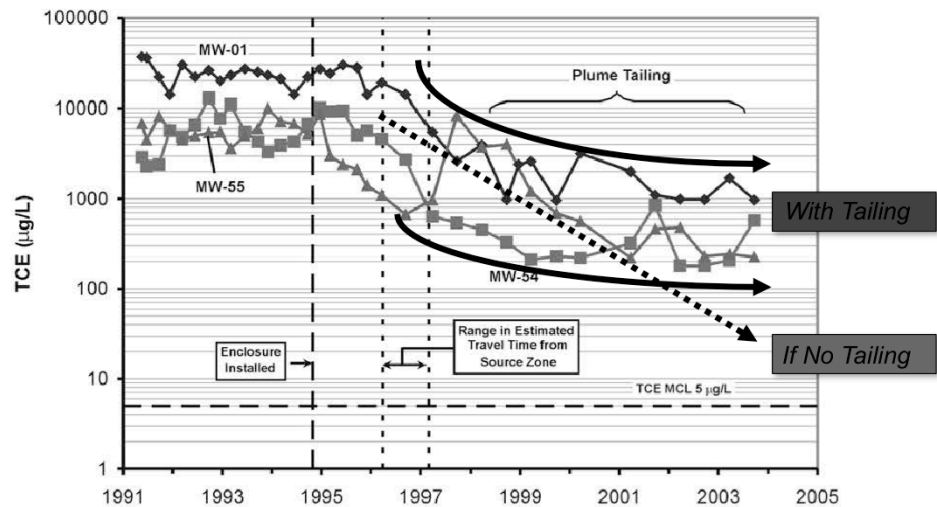
Chapman and Parker, 2005

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Aerial photograph – source area east of facility, monitoring transect along west side of facility 900 ft from source along entire width of facility (~1400 ft).

Concentration vs. Time from Monitoring Wells



Source: Chapman and Parker, 2005 Copyright 2005 American Geophysical Union.
Reproduced/modified by permission of AGU.

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Mini Road Map



◆ **Matrix Diffusion Background**

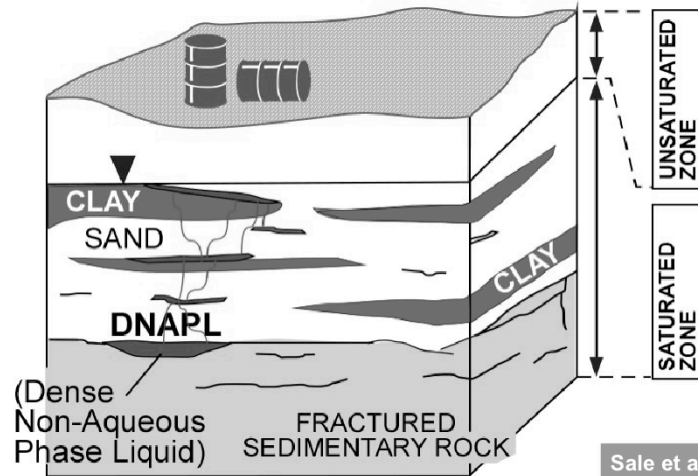
◆ Lines of Evidence

➔ **New Conceptual Model**

◆ Collecting Field Samples

Life Cycle of a Chlorinated Solvent Site

Early Stage



Sale et al., 2008

Life Cycle of a Chlorinated Solvent Site

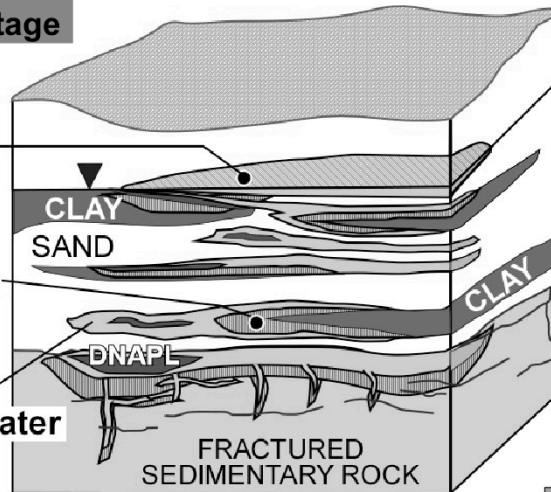
Middle Stage

Vapor
Plume

Matrix
Storage

(Dissolved
and sorbed
phases in
low flow
zones)

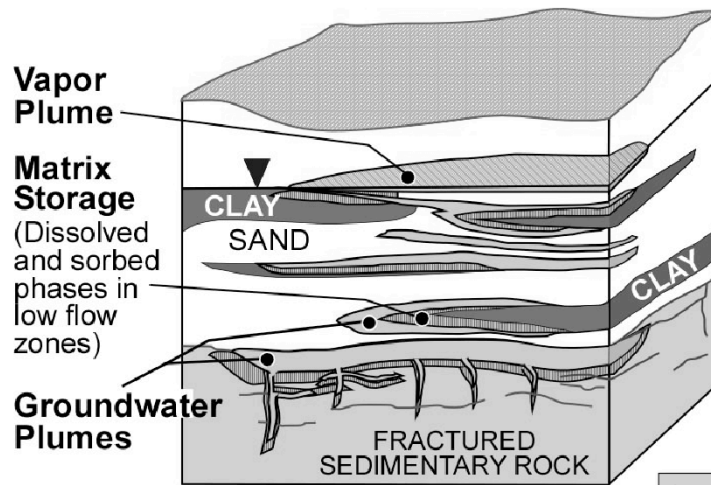
Groundwater
Plumes



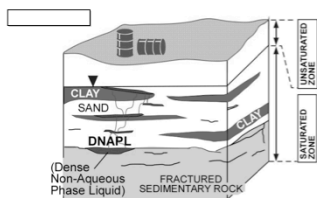
Sale et al., 2008

Life Cycle of a Chlorinated Solvent Site

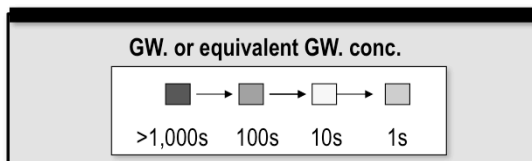
Late Stage



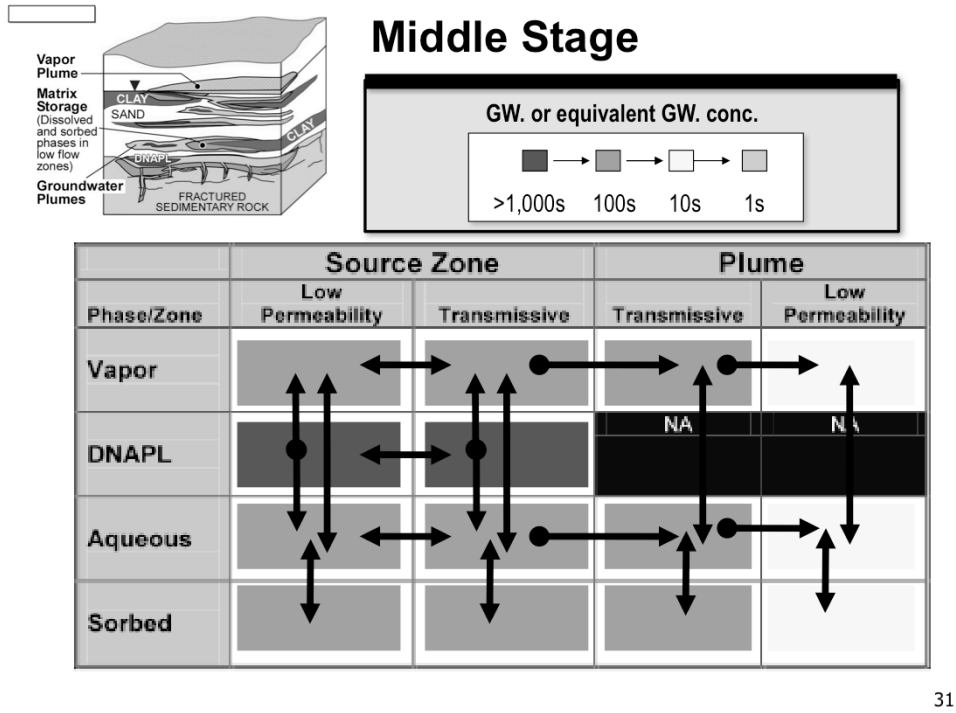
Sale et al., 2008

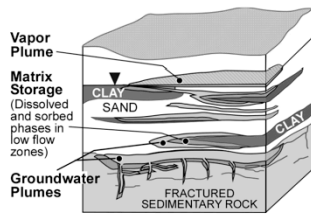


Early Stage

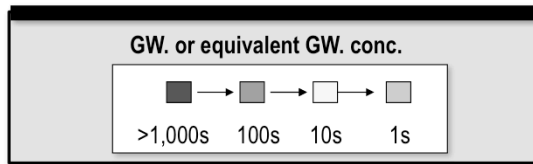


	Source Zone		Plume	
Phase/Zone	Low Permeability	Transmissive	Transmissive	Low Permeability
Vapor				
DNAPL			NA	NA
Aqueous				
Sorbed				

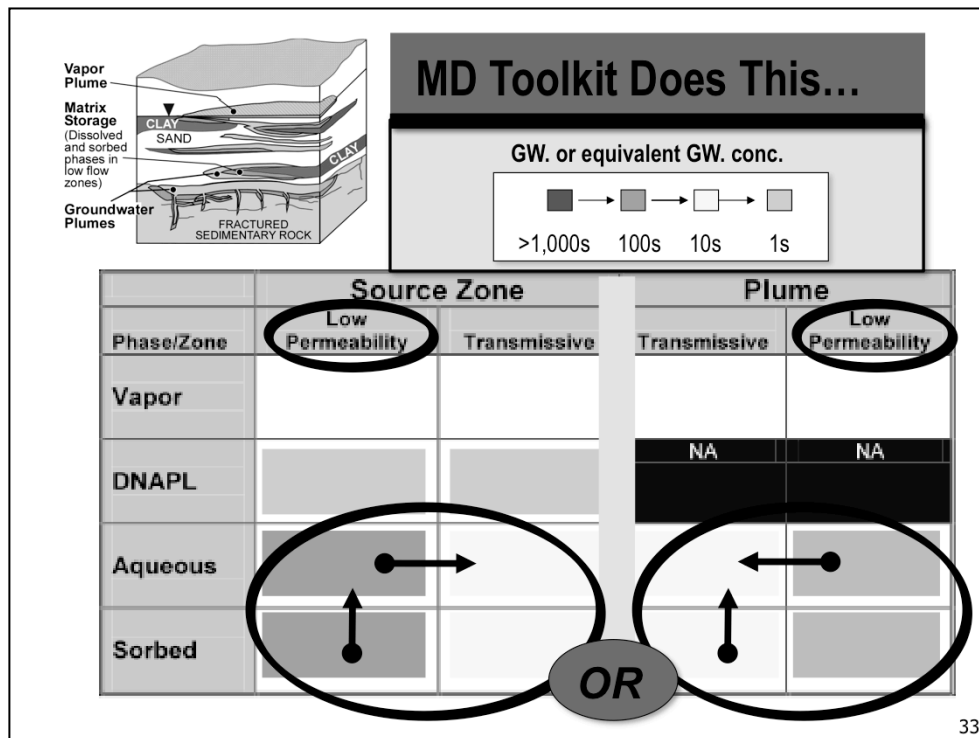




Late Stage



	Source Zone		Plume	
Phase/Zone	Low Permeability	Transmissive	Transmissive	Low Permeability
Vapor	● →	● →	← ●	● ↑
DNAPL	↑	↑	NA	NA
Aqueous	● →	● →	← ●	● ↑
Sorbed	●	●	●	●



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Mini Road Map



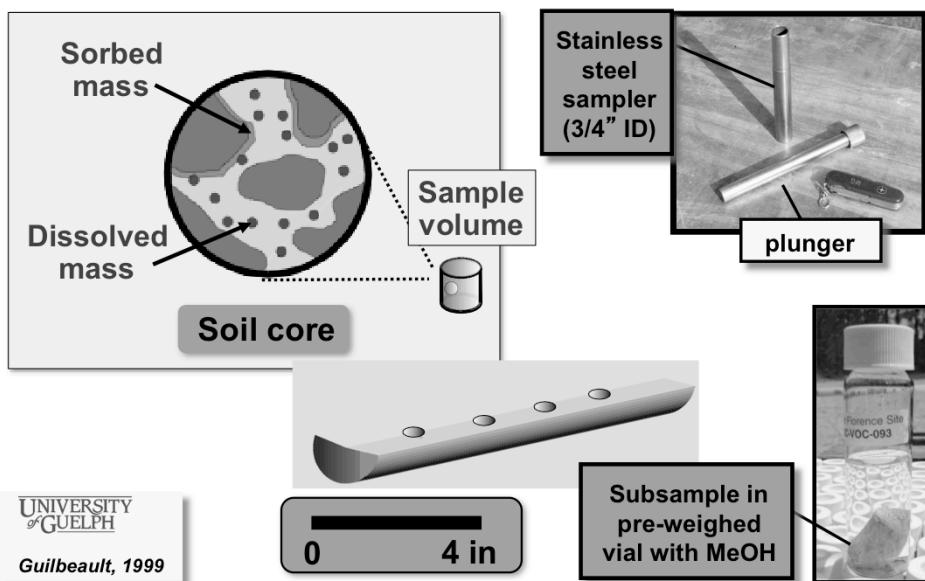
◆ **Matrix Diffusion Background**

◆ Lines of Evidence

◆ New Conceptual Model

➔ **Collecting Field Samples**

High-Resolution Soil Core Subsampling

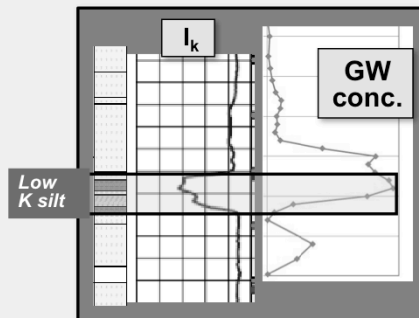


Field Sampling

Step 1. Real-time Profiling to Identify Intervals of Interest

Several tools available, including Waterloo^{APS} (from Stone Environmental Inc.)

- Index of Hydraulic Conductivity (I_k)
- Contaminant concentration and physical-chemical properties through GW sample collection



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Step 2. Soil Subsampling



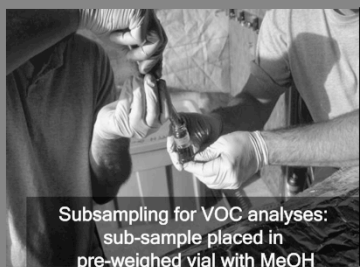
Core contained in aluminum tube or other liner



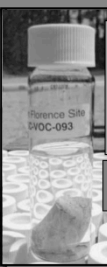
Splitting core tube lengthwise



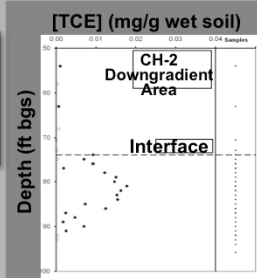
Half of core wrapped in foil to minimize volatilization



Subsampling for VOC analyses: sub-sample placed in pre-weighed vial with MeOH

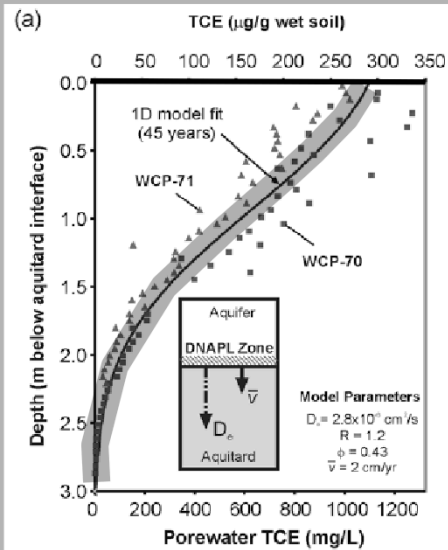


Obtain several high-resolution soil profiles per site

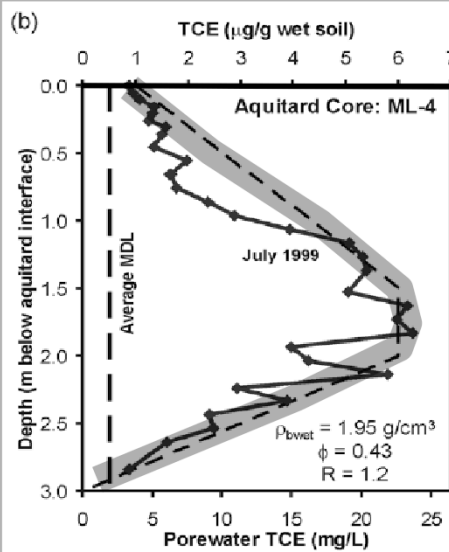


Constant Loading vs. Declining Aquifer Concentration

Zone with DNAPL



Downgradient of Isolated Source



Chapman and Parker, 2005



Exercise

NUMBER 1

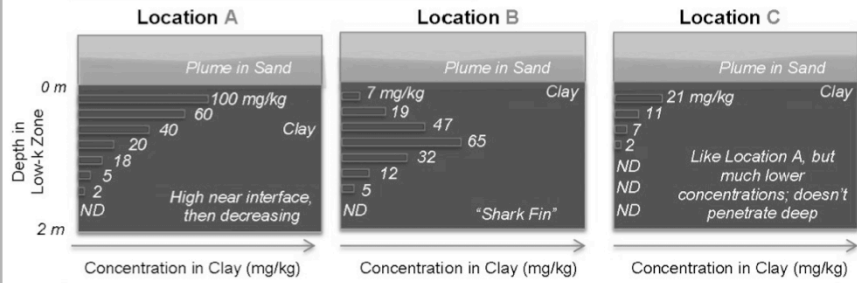
Diffusion Curves



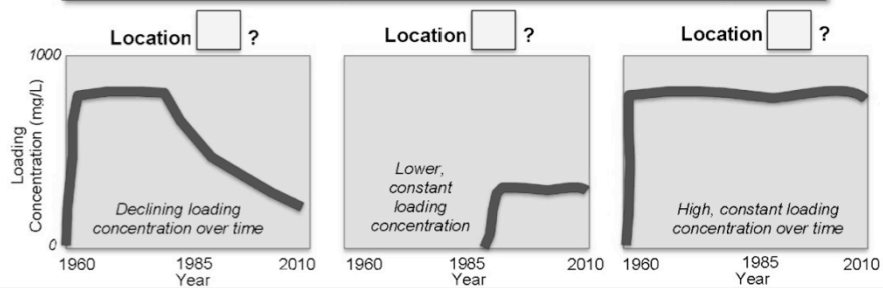
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Match the Curves

Soil Sampling In Clay Results vs. Depth

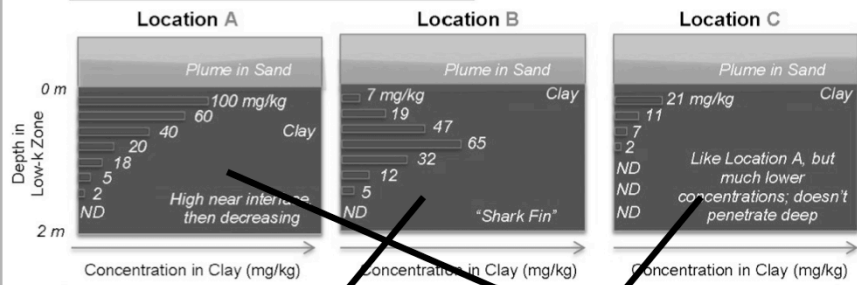


Plume Concentration History That Caused Observed Soil Data in Clay

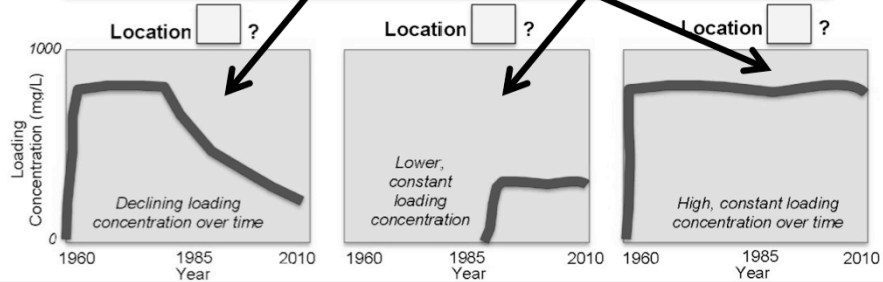


Match the Curves - Answers

Soil Sampling In Clay Results vs. Depth



Plume Concentration History That Caused Observed Soil Data in Clay



Modeling Historical Impacts – Source History Tool



WHAT:

Analytical groundwater model that estimates source concentration over time, i.e., a “source history”

WHERE:

Free download from:

- <http://www.serdp.org> (soon)
- <http://www.gsi-net.com> (now)

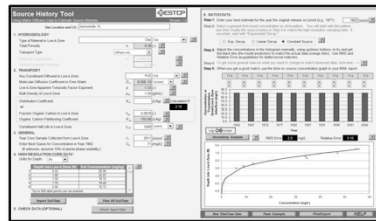
WHO:

S. Farhat, P. de Blanc, C. Newell, and D. Adamson
GSI Environmental Inc.

Project Team: B. Parker and
S. Chapman
University of Guelph

T. Sale
Colorado State University

**Funded by ESTCP
(ER-201032)**



Road Map



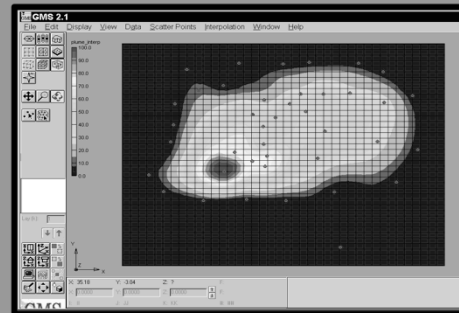
- ◆ Introduction
- ◆ Matrix Diffusion Background
- ➔ **Options for Modeling Matrix Diffusion**
- ◆ Introduction to MDT – Square Root Model
- ◆ Dandy-Sale Model in the MDT
- ◆ Case Study 1
- ◆ Case Study 2
- ◆ Wrap-up

Types of Groundwater Models

- Flow vs. Transport Models

- Numerical Models

- Analytical Models



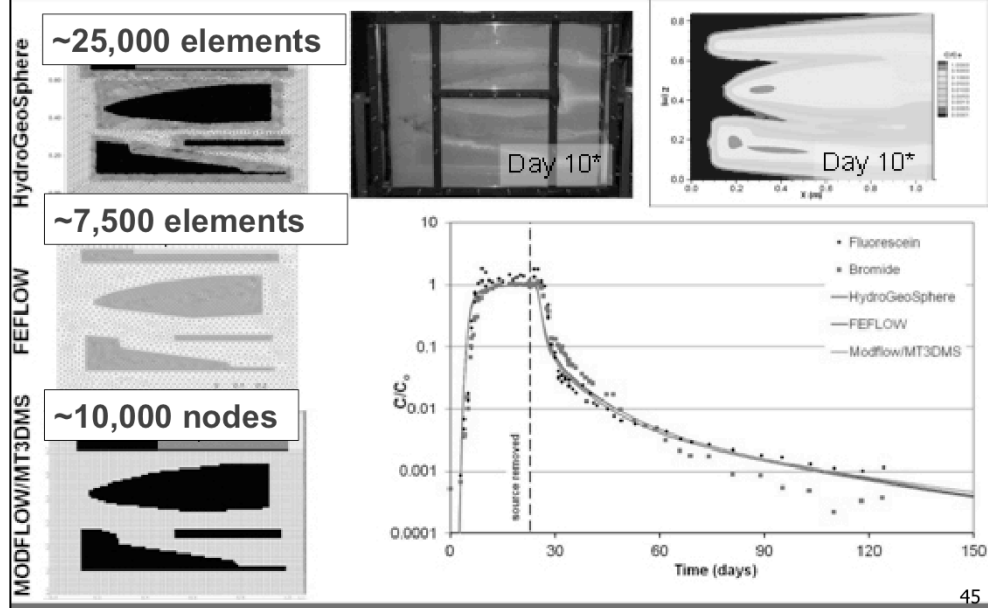
Concentration at Downgradient Distance x Away from Source

$$Conc(x) = \exp \left\{ \frac{x}{2 \alpha_x} \left[1 - \left(1 + \frac{4 \lambda \alpha_x}{Vs/R} \right)^{1/2} \right] \right\} \operatorname{erf} \left[\frac{S_w}{4 \sqrt{\alpha_y x}} \right] \operatorname{erf} \left[\frac{S_d}{4 \sqrt{\alpha_z x}} \right]$$

Longitudinal Dispersivity
Groundwater Seepage Velocity
First-Order Decay Constant
Retardation Coefficient
Hydraulic Conductivity
Effective Soil Porosity
Hydraulic Gradient
Error Function
Transverse Dispersivity
Vertical Dispersivity
Groundwater Source Width and Depth

$Vs = \frac{K i}{n_e}$

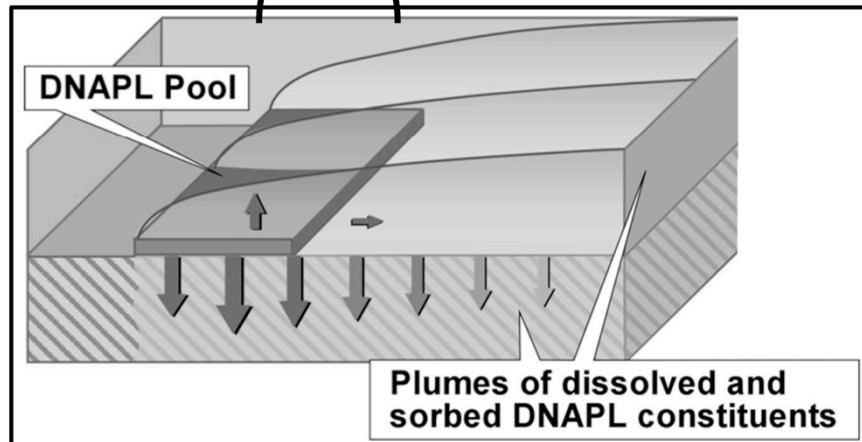
Numerical Models: It takes a lot of grid cells to model this....
 (Chapman, Sale, Doner, Parker, 2012)



Three Simple Analytical Matrix Diffusion Models

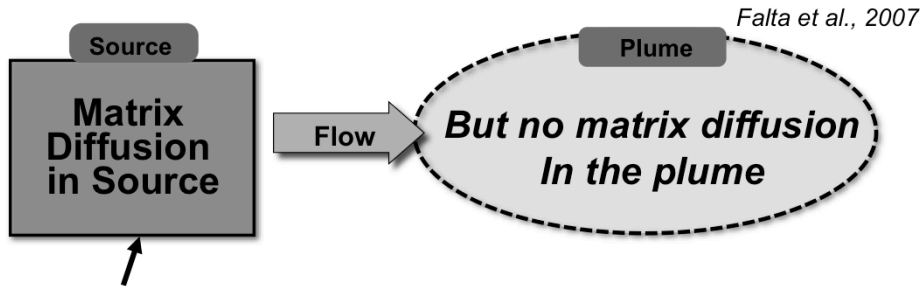
“Square Root” “Dandy-Sale”

REMChlor



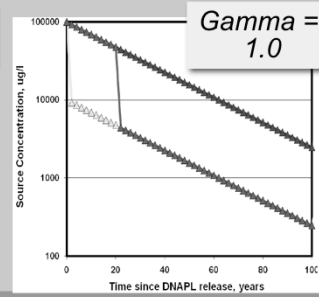
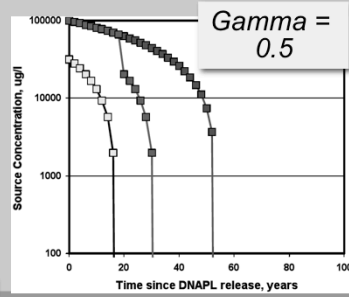
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REMChlor and REMFuel Source/Plume/Remediation Models



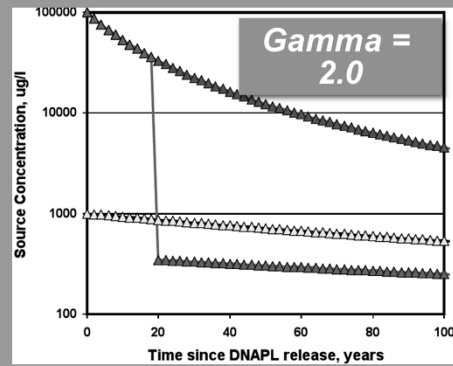
You enter source mass, concentration leaving source
You decide how mass leaves over time with “gamma”
A high gamma (>1.0) can simulate matrix diffusion

REMChlor Model – Effect of Gamma



Can simulate matrix
diffusion in source,
but not plume...

Gamma > 1.0
Gives “long tail”
in source similar
to matrix diffusion



“Square Root Model” for Matrix Diffusion

“On-Off” Source

AFCEE Source Zone Initiative

Final Report

Colorado State University



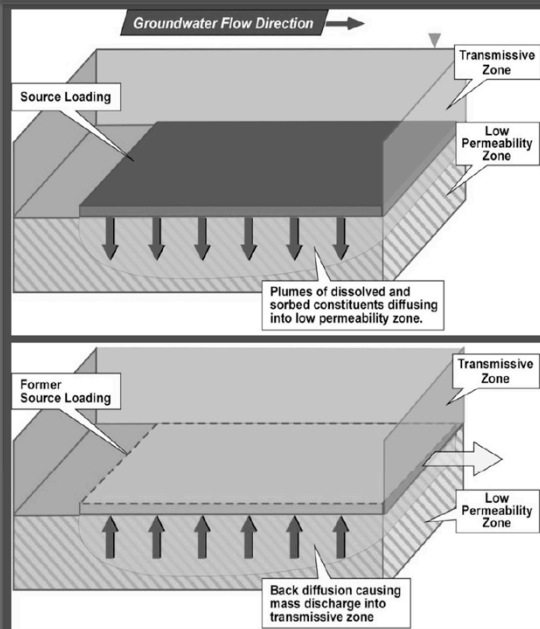
Submitted to

Air Force Center for Environmental Excellence

May 2007

Dr. Tom Sale
Dr. Tissa Illangasekare

Adapted from
Parker et al., 1995



“Square Root” Matrix Diffusion Model

$$M_D = \phi_{LP} C_S L_p \left[\sqrt{\frac{R_{LP} D_e}{\pi t}} - \sqrt{\frac{R_{LP} D_e}{\pi(t-t')}} \right]$$

- M_D : **Mass Discharge** from Low Perm. Unit (grams per day)
assuming no concentration in transmissive zone
- ϕ_{LP} - Low Permeability Unit Porosity
- D_e - Effective Diffusion Coefficient of Low Perm Unit,
- R - Retardation Factor of Low Perm Unit
- t - Time Loading Started, years before simulation time
- t' - Time Loading was Removed, years before simulation time
- C_s - Concentration at interface during loading period

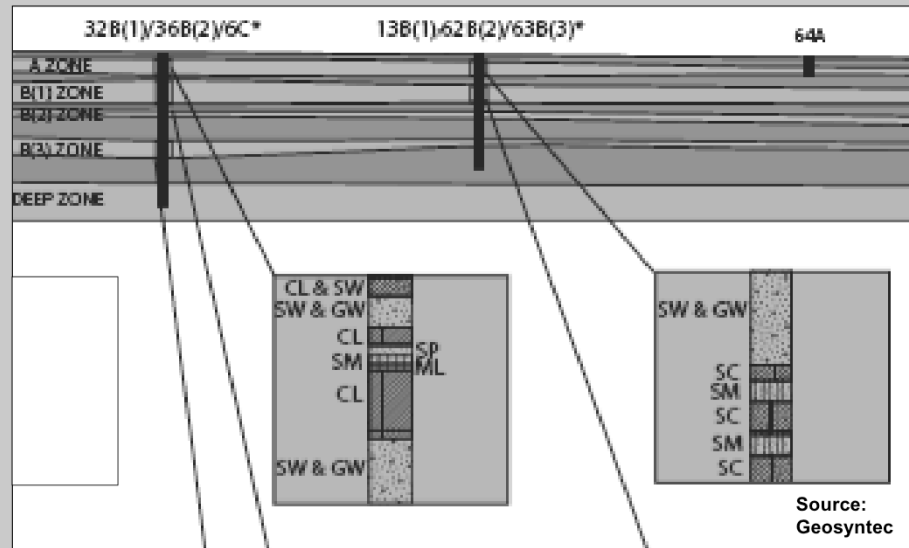
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MEW Site Mountain View, California

Team members: Schlumberger, GSI, Geosyntec
• Seyedabbasi et al., Remediation, 2013
• McDade et al., Remediation, 2013



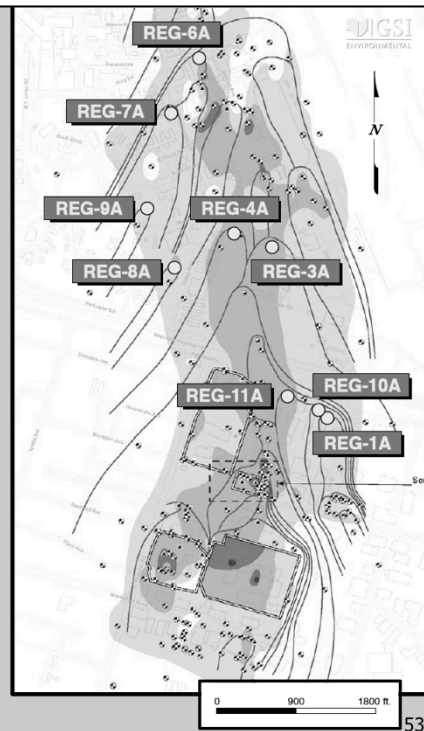
MEW Site: Site Hydrogeology



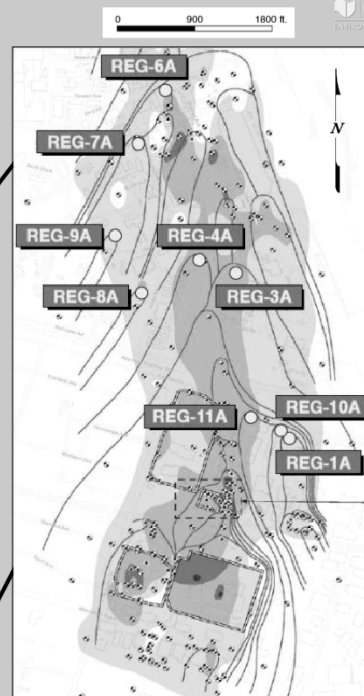
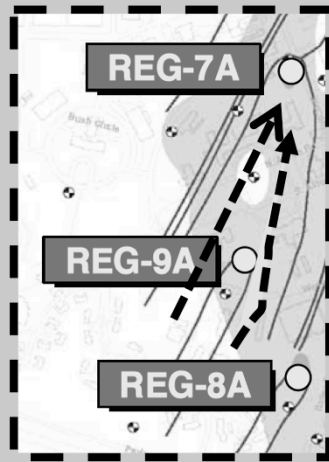
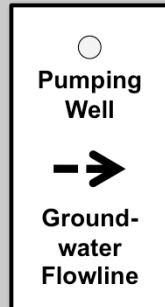
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Pump & Treat System at MEW Site

- Middlefield–Ellis–Whisman Site
- Three Zones: A/A1, B1/A2, B2
- 1980s: Slurry Walls, Pump & Treat
- Today ~100 recovery wells, ~500 gpm
- Removal: ~97,000 pounds VOCs
- Reduction: Approximately 1 OoM decrease in average TCE concentration 1992-2009

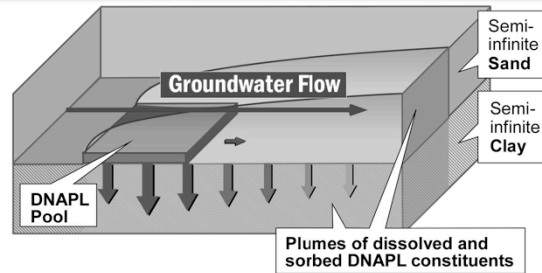


Example A: MEW Site Pump and Treat Capture Zones



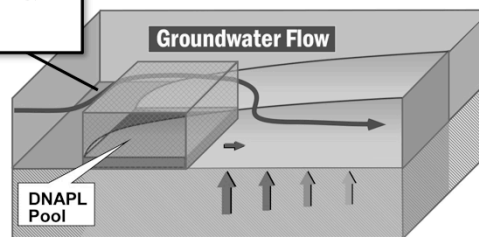
Matrix Diffusion Model Applied to MEW Site

“Charging Period”

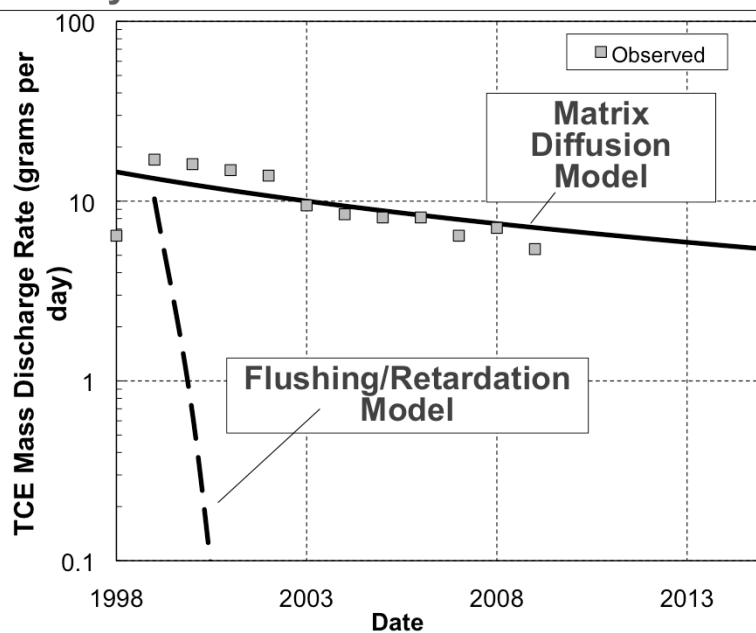


Then Build Slurry Walls, P&T Wells, Contain Sources

“Back Diffusion Period”



Results:
Recovery Well REG-8A: 30 Pore Volumes



Dandy-Sale Model

Vertical Plane Source
(Higher concentration near bottom)



Contents lists available at ScienceDirect

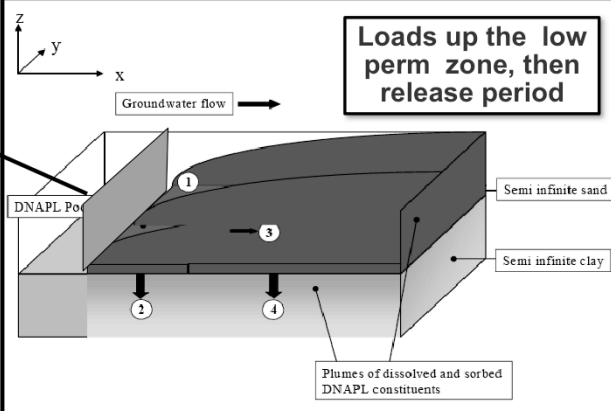
Journal of Contaminant Hydrology

journal homepage: www.elsevier.com/locate/jconhyd



Effects of reduced contaminant loading on downgradient water quality in an idealized two-layer granular porous media

Tom C. Sale^{a,*}, Julio A. Zimbron^{a,1}, David S. Dandy^b



Sale, Zimbron, Dandy, 2008

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Dandy-Sale Analytical Matrix Diffusion Model



Contents lists available at ScienceDirect

Journal of Contaminant Hydrology

journal homepage: www.elsevier.com/locate/jconhyd



Effects of reduced contaminant loading on downgradient water quality in an idealized two-layer granular porous media

Tom C. Sale^{a,*}, Julio A. Zimbron^{a,1}, David S. Dandy^b

^a Department of Civil & Environmental Engineering, Colorado State University, Fort Collins, CO, 80523-1320, United States

^b Department of Chemical & Biological Engineering, Colorado State University, Fort Collins, CO, 80523-1320, United States

$$\frac{C'}{C_0} = \frac{\phi^2}{2\pi} e^{-kx/v} \int_0^x \int_0^{t-x/v} \frac{e^{-k'u}}{\sqrt{u}(x-\xi)^{3/2}} \left[\frac{1}{\sqrt{\pi}\xi} - \frac{b}{\phi} e^{b^2\xi/\phi^2} \operatorname{erfc} \left(\frac{b}{\phi} \sqrt{\xi} \right) \right] \frac{e^{-Y^2 B^2 / (\gamma^2 + 4B^2 u)}}{(\gamma^2 + 4B^2 u)^2} \times \left[4YB^2 u e^{-Y^2 \gamma^2 / 4u (\gamma^2 + 4B^2 u)} + \sqrt{\pi} \gamma \right. \\ \left. (4B^2 u - 2Y^2 B^2 + \gamma^2) \sqrt{\frac{u}{\gamma^2 + 4B^2 u}} \operatorname{erfc} \left(\frac{Y\gamma}{2u} \sqrt{\frac{u}{\gamma^2 + 4B^2 u}} \right) \right] du d\xi \quad (10)$$

1. REMChlor	2. Square Root Model	3. Dandy-Sale Model
Simple	Very simple	Complex Function
Vertical plane source	Horizontal source is directly over low perm zone	Vertical plane source upgradient of low perm zone
No matrix diffusion in plume	<ul style="list-style-type: none"> • On-off source • Unimpeded back diffusion 	<ul style="list-style-type: none"> • On-off source • More accurate back diffusion
Concentration or Mass Discharge	<ul style="list-style-type: none"> • Mass discharge • Mass in low perm • Concentration in Well 	Same as Square Root, but with Conc. in Low Perm.
U.S. EPA CSMoS (Google: "EPA" and "REMChlor")	ESTCP Matrix Diffusion Toolkit (www.gsi-net.com)	

Road Map



- ◆ Introduction
- ◆ Matrix Diffusion Background
- ◆ Options for Modeling Matrix Diffusion
- ➔ **Introduction to MDT – Square Root Model**
- ◆ Dandy-Sale Model in the MDT
- ◆ Case Study 1
- ◆ Case Study 2
- ◆ Wrap-up



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Matrix Diffusion Toolkit



WHAT:

Analytical groundwater transport models that estimates matrix diffusion effects

WHERE:

Free download from:

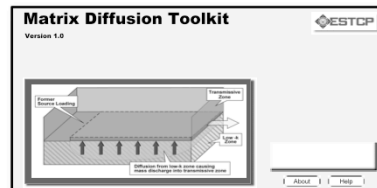
- <http://www.serdp.org>
- <http://www.gsi-net.com>

WHO:

S. Farhat and C. Newell
GSI Environmental Inc.

T. Sale, D. Dandy, and
J. Wahlberg
Colorado State University

Funded by ESTCP



Square Root Model: *Data Input Screen*

SRM Data Input Screen

Matrix Diffusion Toolkit Version 1.0

Site Location and ID:

1. SYSTEM UNITS

☒ SI Units ☐ English Units

2. ANALYSIS TYPE

☐ Source Zone Analysis ☒ Plume Analysis ☐ PRB Analysis ?

3. HYDROGEOLOGY

Low-k Zone Description

Low-k Zone Total Porosity ϕ (-)

Transmissive Zone Darcy Velocity V_d (in/d) ?

4. TRANSPORT - Low-k Zone

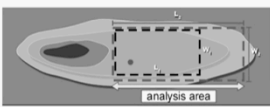
Key Constituent

Molecular Diffusion Coefficient in Free Water D_o (m²/sec)

Apparent Tortuosity Factor Exponent ρ (-)

Retardation Factor R (-) ?

5. PLUME CHARACTERISTICS



High Concentration Zone (Black Box in Picture)

Approximate Length (Length of Black Box) L_1 (m) ?

Approximate Width (Width of Black Box) W_1 (m)

Highest Historical Concentration in Black Box (ug/L)

Concentration of Contour Line in Black Box (ug/L)

Representative Concentration (OK to Override) C_{s1} (ug/L)

Next Highest Concentration Zone (Blue Box in Picture)

Approximate Length (Length of Blue Box) L_2 (m)

Approximate Width (Width of Blue Box) W_2 (m)

5. PLUME CHARACTERISTICS CONT'D

Concentration of Contour Line in Blue Box (ug/L)

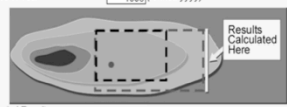
Representative Concentration (OK to Override) C_{s2} (ug/L)

Uncertainty in Plume Concentration Estimations \pm factor of ?

6. GENERAL

Source Loading Starts in Year (format yyyy)

Source Removed in Year (format yyyy)



See Release Period Results

from Year (format yyyy)

to Year (format yyyy)

in Intervals of (yrs)

7. FIELD DATA FOR COMPARISON

Year	1998	1999	2000	2001	2002	2003	2004
Concentration (ug/L)	3832	2371	3162	1957	1000	1468	908
Mass Discharge (g/day)							
Mass (kg)			3000				

DATA INPUT INSTRUCTIONS

☐ Enter value directly.

☒ Value calculated by Toolkit. Do not enter data.

Next Step:

Show Graph

2. ANALYSIS TYPE

☐ Source Zone Analysis

☒ Plume Analysis

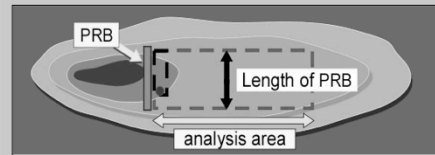
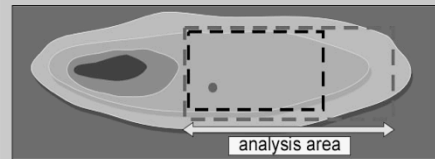
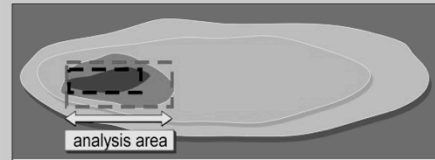
☐ PRB Analysis

?

Select “Source Zone Analysis” to see matrix diffusion impacts in a source zone:

Select “Plume Analysis” to see matrix diffusion impacts in a downgradient plume:

Select “PRB Analysis” to see matrix diffusion impacts downgradient of a PRB:



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3. HYDROGEOLOGY

Low-k Zone Description

Low-k Zone Total Porosity

Transmissive Zone Darcy Velocity

Silt

Silt

ϕ

0.43

(-)

V_d

0.13

(m/d)

Calculate V_d

?

Low-k Zone Description	Choose from dropdown menu or enter directly
Low-k Zone Total Porosity	Keep Toolkit default or enter directly. • Based on Pankow and Cherry (1996) • Domenico and Schwartz (1999) • Davis (1969) and Johnson and Morris (1962)
Transmissive Zone Darcy Velocity	Enter directly or use Toolkit to calculate

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Square Root Model: *Transport*

4. TRANSPORT - Low-k Zone

Key Constituent

Molecular Diffusion Coefficient in Free Water

Apparent Tortuosity Factor Exponent

Retardation Factor

	TCE	TCE	
D_o	9.10E-10	(m2/sec)	
p	3.30E-01	(-)	
R	1.20	(-)	Calculate R ?

Parameter	Description
Molecular Diffusion Coefficient in Free Water	Keep Toolkit default or enter directly <ul style="list-style-type: none"> • From TRRP (2008) <ul style="list-style-type: none"> • TCE = 9.1E-06 cm²/s • PCE = 8.2E-06 cm²/s • Benzene = 9.8E-06 cm²/s • Other refs: Pankow and Cherry (1996), Wiedemeier <i>et al.</i> (1999), etc.

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Apparent Tortuosity Factor Exponent

Parameter	Description
Apparent Tortuosity Factor Exponent	Keep Toolkit default or enter directly

tortuosity $\tau = n^p$ porosity

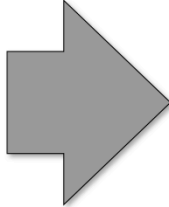
p varies:

- 1/3: Millington, 1959
- 0.3 to 1.5: Charbeneau, 2000
- 1.3 to 4.5: Pankow and Cherry, 1997
- 0.33 for Clay: Parker et al., 1994

GSI's Decision Support for Tortuosity

(1) Pick Material

- Gravel
- Sand
- Silt
- Clay
- Sandstone/Shale
- Granite



(2) Software Produces

If no porosity value is entered:

- Default Porosity
- Tortuosity factor

If porosity value is entered:

- Tortuosity factor

Current Look-up Table

Soil Type	Default Porosity	Relationship*	Estimated Tortuosity
Fine Sand	0.20	$\tau = n^{0.33}$	0.59
Silt	0.48	$\tau = n^{1.1}$	0.45
Clay	0.47	$\tau = n^{1.1}$	0.44
Sandstone/ Shale	0.10	$\tau = n$	0.10
Granite	0.006	$\tau = n^{0.55}$	0.06

* From Parker et al. (2004); Millington and Quirk (1961); and Pankow and Cherry (1996)

Retardation Factor

Parameter	Description
Retardation Factor	Enter directly or use Toolkit to calculate <ul style="list-style-type: none">• Transmissive zones<ul style="list-style-type: none">1-3 (typical for BTEX)2-5 (typical for CVOC)• Low-k zones<ul style="list-style-type: none">Thought to be > trans zones. Currently, few sites with data

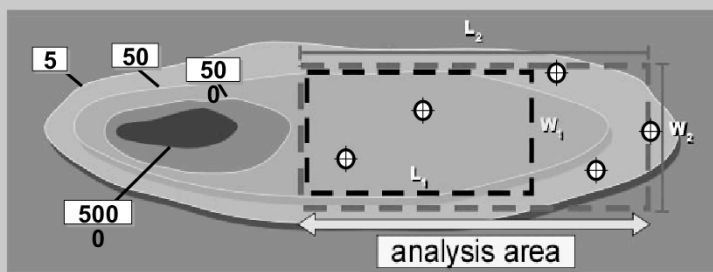
Calculating Retardation Factor

Parameter	Description
K_{oc}	Keep Toolkit default or enter directly <ul style="list-style-type: none">• From TRRP (2008)<ul style="list-style-type: none">• TCE = 93 mL/g• PCE = 155 mL/g• Benzene = 66 mL/g• Other refs: Pankow and Cherry (1996), Wiedemeier <i>et al.</i> (1999), etc.

Calculating Retardation Factor Cont'd

Parameter	Description
Low-k zone fraction organic carbon	<p>Enter directly</p> <ul style="list-style-type: none"> • Likely range: 0.0002 - 0.10 • Chapman and Parker (2005): silts and clays = 0.0024 to 0.00104 • Adamson (2012): clay = 0.001; silts = <0.0005 to 0.0022
Soil bulk density of low-k zone	<p>Enter directly</p> <ul style="list-style-type: none"> • Typical value = 1.7 g/mL • Lovanh et al. (2000) and Domenico and Schwartz (1990): <ul style="list-style-type: none"> Clay = 1.0 to 2.4 Sandstone = 1.6 to 2.68 • Koerner (1984): <ul style="list-style-type: none"> Stiff glacial clay = 2.07 organic clay = 1.43

Square Root Model: *Plume Charac.*



High Concentration Zone (Black Box in Picture)

Approximate Length (Length of Black Box)

Approximate Width (Width of Black Box)

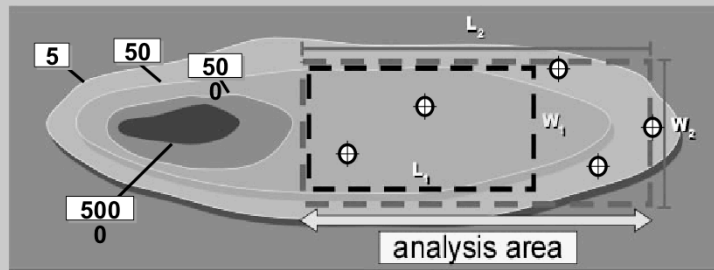
Highest Historical Concentration in Black Box

Concentration of Contour Line in Black Box

Representative Concentration (OK to Override)

L_1	3.30E+02 (m)	<input data-bbox="1177 703 1209 745" type="text" value="?"/>
W_1	3.00E+02 (m)	
	3.70E+04 (ug/L)	<input data-bbox="1120 787 1177 829" type="text" value="3.70E+04"/>
	3.70E+04 (ug/L)	
C_{s1}	3.70E+04 (ug/L)	<input data-bbox="1201 871 1266 903" type="button" value="Restore"/>

Plume Characteristics Cont'd



Next Highest Concentration Zone (Blue Box in Picture)

Approximate Length (Length of Blue Box)

L_2 (m)

Approximate Width (Width of Blue Box)

W_2 (m)

Concentration of Contour Line in Blue Box

(ug/L)

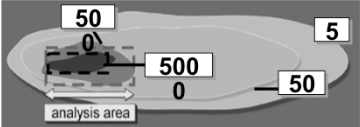
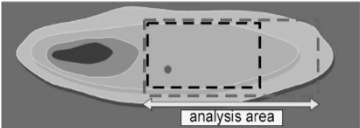
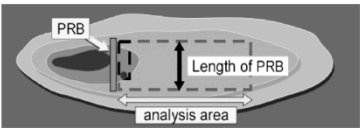
Representative Concentration (OK to Override)

C_{s2} (ug/L)

[Restore](#)

Uncertainty in Plume Concentration Estimations

\pm factor of

Type of Problem to Be Analyzed Using the Toolkit	Black Box in Drawing	Blue Box in Drawing
<p>To see matrix diffusion impacts in a source zone:</p> 	<p>Is drawn around the highest contour in the source area.</p>	<p>Is drawn around the second highest contour in the source area.</p>
<p>To see matrix diffusion impacts in a downgradient plume:</p> 	<p>Is drawn around the highest contour downgradient of the source area.</p>	<p>Is drawn around the second highest contour downgradient of the source area.</p>
<p>To see matrix diffusion impacts downgradient of a PRB:</p> 	<p>Is drawn around the highest contour downgradient of the PRB. The width of the box is the width of the PRB.</p>	<p>Is drawn around the second highest contour downgradient of the PRB. The width of the box is the width of the PRB.</p>

Square Root Model: *General*

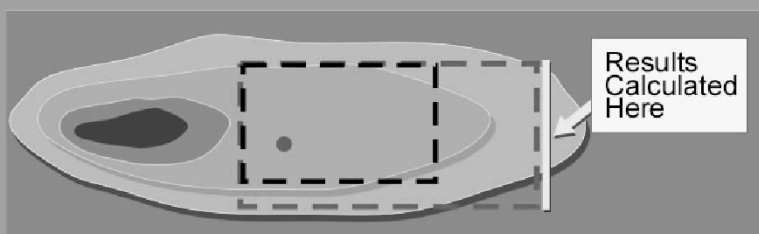
6. GENERAL

Source Loading Starts in Year

1952 (format: yyyy)

Source Removed in Year

1996 (format: yyyy)



See Release Period Results

from Year

1991 (format: yyyy)

to Year

2005 (format: yyyy)

in Intervals of

1 (yrs)

Square Root Model: *Field Data*

7. FIELD DATA FOR COMPARISON

Year	1998	1999	2000	2001	
Concentration (ug/L)	3832	2371	3162	1957	
Mass Discharge (g/day)					
Mass (kg)			3000		

- Can enter up to 8 values for comparison
 - Helps with model calibration

SRM Output

- Mass discharge

- Concentration in transmissive zone

- Mass in low-k zone

SRM = Square Root Model

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Road Map



- ◆ Introduction
- ◆ Matrix Diffusion Background
- ◆ Options for Modeling Matrix Diffusion
- ◆ Introduction to MDT – Square Root Model
- ➔ **Dandy-Sale Model in the MDT**
- ◆ Case Study 1
- ◆ Case Study 2
- ◆ Wrap-up

Dandy-Sale Model: Data Input Screen

DSM Data Input Screen

Main Diffusion Toolkit Version 1.0

Site Location and ID:

1. SYSTEM UNITS

☒ SI Units ☐ English Units

2. HYDROGEOLOGY

Transmissive Zone Description:

Transmissive Zone Effective Porosity: (-)

Low-k Zone Description:

Low-k Zone Total Porosity: (-)

Transmissive Zone Seepage Velocity: (m/d)

3. TRANSPORT

Key Constituent (enter directly or choose from drop down list):

Plume Loading Concentration Immediately Above Low-k Zone in Vertical Plane Source During Loading Period: (mg/L)

Molecular Diffusion Coefficient in Free Water: (m²/sec)

Transmissive Zone Apparent Tortuosity Factor Exponent: (-)

Low-k Zone Apparent Tortuosity Factor Exponent: (-)

Bulk Density of Transmissive Zone: (g/mL)

Bulk Density of Low-k Zone: (g/mL)

Distribution Coefficient: (mL/g)

or

Transmissive Zone Fraction of Organic Carbon: (-)

Low-k Zone Fraction of Organic Carbon: (-)

Organic Carbon Partitioning Coefficient: (L/kg)

4. SOURCE ZONE CHARACTERISTICS

Source Zone Length: 32.1 (m)

Source Zone Width: 38.3 (m)

Transverse (Vertical) Hydrodynamic Dispersionity: 1.00E-01 (m)

Source Loading Starts in Year: (format: yyyy)

Source Removed in Year: (format: yyyy)

5. GENERAL

See Release Period Results for:

Year: (format: yyyy)

Lateral Distance from Source: 280 (m)

Depth into Low-k Zone: 3 (m)

DATA INPUT INSTRUCTIONS

☐ Enter value directly.

☒ Value calculated by Toolkit. Do not enter data.

Next Step:

Dandy-Sale Model: *Hydrogeology*

2. HYDROGEOLOGY

Transmissive Zone Description

Transmissive Zone Effective Porosity

Low-k Zone Description

Low-k Zone Total Porosity

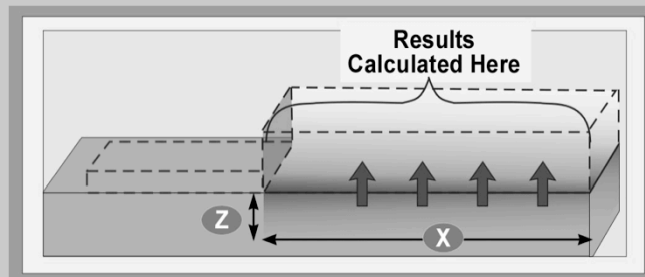
Transmissive Zone Seepage Velocity

	Sand	Sand	▼
n_e	0.35	(-)	
	Silt	Silt	▼
n'	0.43	(-)	
V	3.70E-01	(m/d)	▼
		Calculate V	?

■ Similar to SRM Data Input

- Choose from dropdown menu or enter directly
- Keep Toolkit default or overwrite
- Enter directly or use Toolkit to calculate value

Dandy-Sale Model: *General*



5. GENERAL

See Release Period Results for:

Year

2000 (format: yyyy)

Lateral Distance from Source

x 280 (m)

Depth into Low-k Zone

z 3 (m)

Dandy-Sale Model: *Outputs*

Low-k Zone

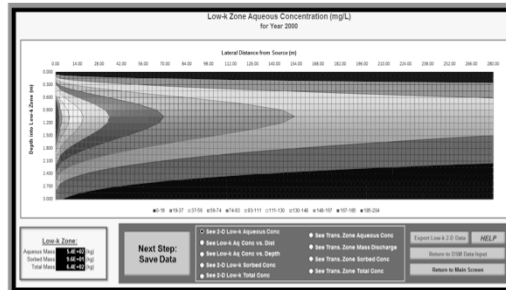
- 2-D aqueous concentration
- Aqueous concentration vs. distance
- Aqueous concentration vs. depth
- 2-D sorbed concentration
- 2-D total concentration

Transmissive Zone

- Aqueous concentration
- Mass discharge
- Sorbed concentration
- Total concentration

Aqueous, Sorbed, and Total Mass

- Low-k zone
- Transmissive zone



Road Map



- ◆ Introduction
- ◆ Matrix Diffusion Background
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- ◆ Introduction to MDT – Square Root Model
- ◆ Dandy-Sale Model in the MDT
- ➔ **Case Study 1**
- ◆ Case Study 2
- ◆ Wrap-up



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Plume persistence due to aquitard back diffusion following dense nonaqueous phase liquid source removal or isolation

Steven W. Chapman and Beth L. Parker

Department of Earth Sciences, University of Waterloo, Waterloo, Ontario, Canada

Received 28 April 2005; revised 18 July 2005; accepted 4 August 2005; published 6 December 2005.

[1] At an industrial site on a sand aquifer overlying a clayey silt aquitard in Connecticut, a zone of trichloroethylene dense nonaqueous phase liquid (DNAPL) at the aquifer bottom was isolated in late 1994 by installation of a steel sheet piling enclosure. In response to this DNAPL isolation, three aquifer monitoring wells located approximately 330 m downgradient exhibited strong TCE declines over the next 2–3 years, from trichloroethylene (TCE) concentrations between 5000 and 30,000 $\mu\text{g/L}$ to values leveling off between 200 and 2000 $\mu\text{g/L}$. TCE concentrations from analysis of vertical cores from the aquitard below the plume and also from depth-discrete multilevel systems in the aquifer sampled in 2000 were represented in a numerical model. This shows that vertical back diffusion from the aquitard combined with horizontal advection and vertical transverse dispersion account for the TCE distribution in the aquifer and that the aquifer TCE will remain much above the MCL for centuries.

Citation: Chapman, S. W., and B. L. Parker (2005), Plume persistence due to aquitard back diffusion following dense nonaqueous phase liquid source removal or isolation, *Water Resour. Res.*, 41, W12411, doi:10.1029/2005WR004224.

1. Introduction

[2] It has long been recognized that DNAPL zones in aquifers cause persistent plumes composed of dissolved phase contaminants [Schwille, 1988; Mackay and Cherry, 1989]. Decades of experience indicates pump and treat fails to achieve permanent aquifer restoration due to the presence

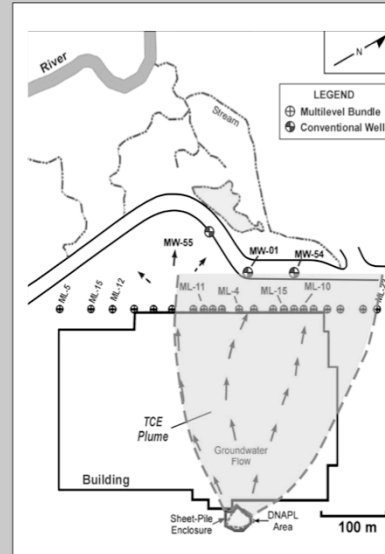
source removal or isolation if low-permeability zones are present within the aquifer, or at the top and/or bottom of the aquifer.

[3] A common situation at contaminated sites is the presence of a DNAPL accumulation zone at the bottom of unconfined sand or gravel aquifers underlain by clayey

Case Study #1: *Industrial Site, CT*

Site from Chapman and Parker, 2005

- Metal product manufacturing site (1952 – 2001)
- TCE occurs in surficial sandy aquifer
 - overlying a clayey silt aquitard
- TCE DNAPL isolated in 1994 using steel sheet pile enclosure
- Historical industrial pumping resulted in a long-term downward hydraulic gradient across the aquitard
- In 2000, TCE observed in
 - Vertical cores collected from aquitard below plume
 - Depth-discrete multilevel sampling



Case Study #1: *Industrial Site, CT*

Matrix Diffusion Toolkit used to:

- Estimate effects of diffusion into and from low-k zones
- Both SRM and DSM applied
 - **Step 1:** Initial values entered into the Toolkit
 - **Step 2:** Toolkit outputs compared to field observed TCE

SRM: *Site-specific Parameters*

Parameter	Value
Low-k porosity	0.43
Darcy velocity	0.13 m/d
Retardation factor	1.2
Representative concentration	37,000 ug/L (max observed)
Conc. zone dimensions	330 m x 300 m
Source starts	1952
Source removed	1996 (“effective”)
Mol. Diff. coeff. (Toolkit default)	$9.1 \times 10^{-10} \text{ m}^2/\text{sec}$
App. tort. fac. exp.	0.42

SRM: Input Screen

SRM Data Input Screen

Version 1.2

Site Location and ID:

1. SYSTEM UNITS

☒ SI Units ☐ English Units

2. ANALYSIS TYPE

☐ Source Zone Analysis ☒ Plume Analysis ☐ PRB Analysis ?

3. HYDROGEOLOGY

Low-k Zone Description: or

Low-k Zone Total Porosity: (?)

Transmissive Zone Darcy Velocity: (m/d) Calculate Vd ?

4. TRANSPORT - Low-k Zone

Key Constituent: or

Molecular Diffusion Coefficient in Free Water: (m²/sec)

Apparent Tortuosity Factor Exponent: (?)

Retardation Factor: (?) Calculate R ?

5. PLUME CHARACTERISTICS

High Concentration Zone (Black Box in Picture)

Approximate Length (Length of Black Box): (m) ?

Approximate Width (Width of Black Box): (m)

Highest Historical Concentration in Black Box: (ug/L)

Concentration of Contour Line in Black Box: (ug/L)

Representative Concentration (OK to Override): (ug/L) Restore

Next Highest Concentration Zone (Blue Box in Picture)

Approximate Length (Length of Blue Box): (m)

Approximate Width (Width of Blue Box): (m)

5. PLUME CHARACTERISTICS CONT'D

Concentration of Contour Line in Blue Box: (ug/L)

Representative Concentration (OK to Override): (ug/L) Restore

Uncertainty in Plume Concentration Estimations: \pm factor of ?

6. GENERAL

Source Loading Starts in Year: (format: yyyy)

Source Removed in Year: (format: yyyy)

See Release Period Results

from Year: (format: yyyy)

to Year: (format: yyyy)

in Intervals of: (yrs)

7. FIELD DATA FOR COMPARISON

Year	1998	1999	2000	2001	2002	2003	2004
Concentration (ug/L)	3832	2371	3162	1957	1000	1468	908
Mass Discharge (g/day)							
Mass (kg)			3000				

Next Step:

Show Graph

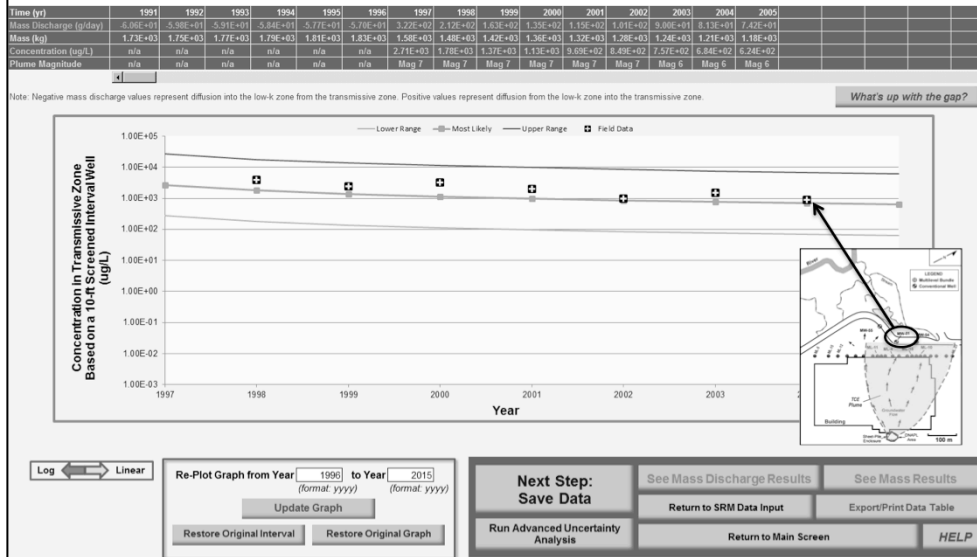
DATA INPUT INSTRUCTIONS

☐ Enter value directly.

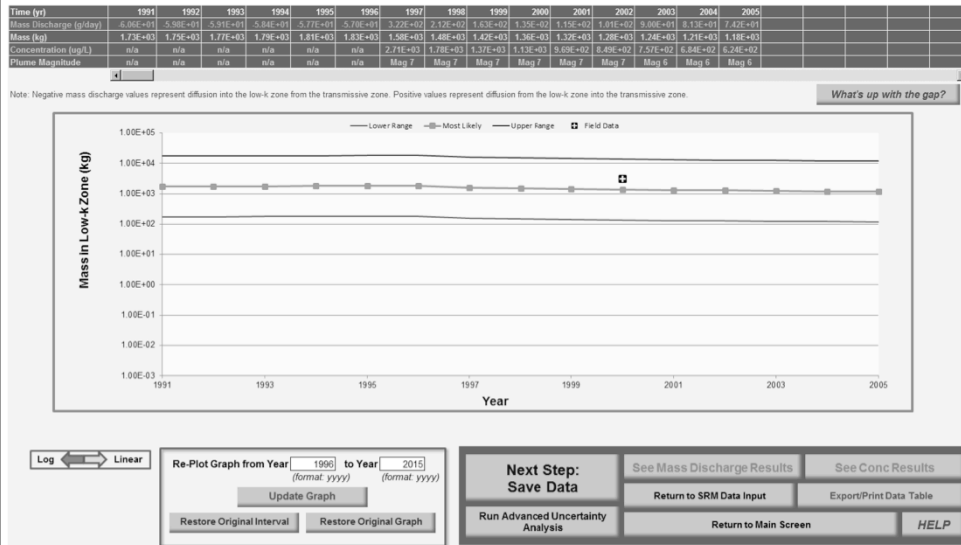
☒ Value calculated by Toolkit. Do not enter data.

New Site/Clear Data **Paste Example** **HELP**

SRM: Concentration Output



SRM: Mass in Low-k Zone



SRM: *Output*

Time (yr)	2535	4	2555	2556	2557
Mass Discharge (g/day)	6.27E-01	1	5.95E-01	5.93E-01	5.92E-01
Mass (kg)	2.57E+02	2	2.52E+02	2.52E+02	2.52E+02
Concentration (ug/L)	5.28E+00	3	5.01E+00	4.99E+00	4.98E+00
Plume Magnitude	Mag 4	4	Mag 4	Mag 4	Mag 4

■ Estimate of Time to Clean

- > 500 years to reach MCL of 5 ug/L

Case Study #1: *SRM Key Points*

- Matrix Diffusion Toolkit reproduced **observed concentrations** within an order of magnitude
- No adjustment needed for Toolkit default parameters
- Matrix Diffusion Toolkit reproduced **observed mass in low-k zone** within an order of magnitude
- SRM modeling estimates >500 yr to reach MCL of 5 ug/L
 - Compares well to Chapman and Parker's more sophisticated modeling that indicated concentrations "will remain much above the MCL for centuries."
- Typical advection-dispersion type model would show no mass in the low-k unit, a fundamentally incorrect conceptual model

MCL = Maximum Contaminant Level

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Road Map



- ◆ Introduction
- ◆ Matrix Diffusion Background
- ◆ Options for Modeling Matrix Diffusion
- ◆ Introduction to MDT – Square Root Model
- ◆ Dandy-Sale Model in the MDT
- ◆ Case Study 1
- ➔ **Case Study 2**
- ◆ Wrap-up



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Case Study #2: *DSM Modeling*

- Same site as Case Study #1
- DSM used to estimate effects of diffusion into and from low-k zones
- Estimate groundwater concentrations in the low-k zone
 - Source area
 - Plume area
- Modeling approach:
 - **Step 1:** Initial values entered into the Toolkit
 - **Step 2:** Toolkit outputs compared to field observed TCE values

DSM: *Site-specific Parameters*

Parameter	Value
Low-k (silt) porosity	0.43
Trans zone (sand) porosity	0.35
Seepage velocity	0.37 m/d
Mean concentration	1100 mg/L (TCE solubility)
Trans zone bulk density	1.7 g/mL
Low-k zone bulk density	1.5 g/mL

DSM: *Site-specific Parameters*

Parameter	Value
Trans zone foc	0.038%
Low-k zone foc	0.054%
Conc. zone dimensions	32 m x 39 m
Source starts	1952
Source removed	1997

foc = fraction organic carbon

DSM: *Toolkit Default Parameters*

Parameter	Value
Mol. diff. coeff.	$9.1 \times 10^{-10} \text{ m}^2/\text{sec}$
Trans zone app. tort. fac. exp.	0.33
Low-k zone app. tort. fac. exp.	0.42
Organic carbon part. coeff.	93.3 L/kg
Coeff. Transverse hyd. disp	0.16

Source Evaluation

DSM Data Input Screen

Matrix Diffusion Toolkit Version 1.2

Site Location and ID

1. SYSTEM UNITS

☒ SI Units ☐ English Units

2. HYDROGEOLOGY

Transmissive Zone Description

Transmissive Zone Effective Porosity n_e (-)

Low-k Zone Description

Low-k Zone Total Porosity n' (-)

Transmissive Zone Seepage Velocity V (m/s) ?

3. TRANSPORT

Key Constituent (enter directly or choose from drop down list)

Plume Loading Concentration Immediately Above Low-k Zone in Vertical Plane Source During Loading Period C_p (mg/L)

Molecular Diffusion Coefficient in Free Water D_w (m²/sec)

Transmissive Zone Apparent Tortuosity Factor Exponent p (-)

Low-k Zone Apparent Tortuosity Factor Exponent p' (-)

Bulk Density of Transmissive Zone ρ_b (g/ml)

Bulk Density of Low-k Zone ρ'_b (g/ml)

Distribution Coefficient K_d (mL/g)

or

Transmissive Zone Fraction of Organic Carbon f_{oc} (-)

Low-k Zone Fraction of Organic Carbon f'_{oc} (-)

Organic Carbon Partitioning Coefficient K_{oc} (L/kg)

DATA INPUT INSTRUCTIONS

☐ Enter value directly.

☒ Value calculated by Toolkit. Do not enter data.

DNAPL Source

Transmissive Zone

Low-k Zone

"L" is only used to define the vertical concentration for the vertical plane source.

Results Calculated Here

4. SOURCE ZONE CHARACTERISTICS

Source Zone Length L (m)

Source Zone Width W (m)

Transverse (Vertical) Hydrodynamic Dispersivity α_v (m) ?

Source Loading Starts in Year (format: yyyy)

Source Removed in Year (format: yyyy)

5. GENERAL

See Release Period Results for:

Year (format: yyyy)

Lateral Distance from Source x (m)

Depth into Low-k Zone z (m)

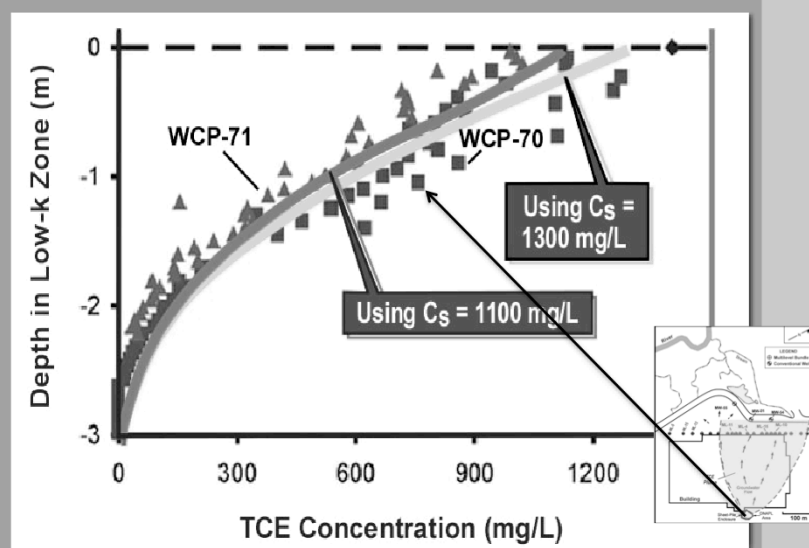
Next Step: Show Graph

Return to Model Selection Screen

Return to Main Screen

Help

Comparison of DSM with Observed

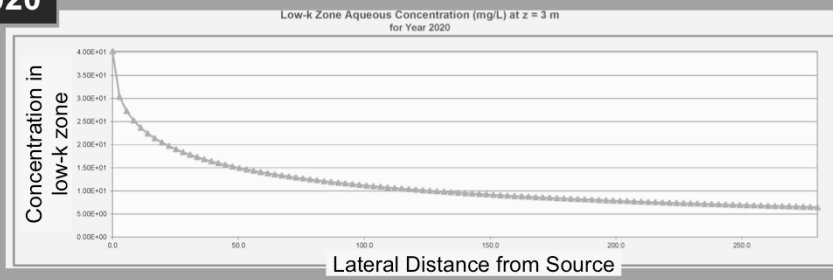


Case Study #2: *Key Points*

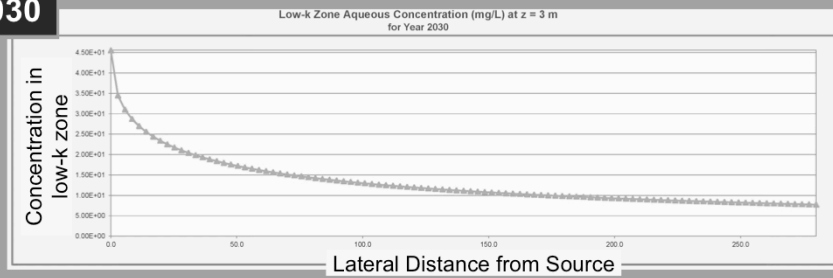
- Matrix Diffusion Toolkit reproduced **observed concentrations** reasonably well
- Comparison using max reported source concentration of 1300 mg/L
 - ▶ Also reproduced **observed concentrations** reasonably well
- No adjustment needed for Toolkit default parameters

Future Predictions

2020



2030



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Road Map



- ◆ Introduction
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➔ **Wrap-up**

Which model should I use: SRM or DSM?

I Want the Following Information:	Which Model?	Output
1. Mass Discharge (sometimes called mass flux) data from a low-k zone to a transmissive zone in units of grams per day versus time (both past and future).	Square Root OR Dandy-Sale	Mass discharge vs. time plot
2. How much mass could be present in low-k zones at my site?	Square Root OR Dandy-Sale	Mass in low-k zone vs. time plot

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Which model should I use: SRM or DSM?

I Want the Following Information:	Which Model?	Output
3. If I install a permeable reactive barrier, will I have trouble achieving downgradient cleanup standards?	Square Root OR Dandy-Sale	Concentration* vs. time plot or mass discharge vs. time plot
4. I want to know the concentration vs. depth profile in a low-k zone.	Dandy-Sale	Concentration* vs. depth plot or Concentration vs lateral distance plot

* Concentration assuming a monitoring well with a 10-foot screened interval (this cannot be changed in the model)

Which model should I use: SRM or DSM?

I Want the Following Information:	Which Model?	Output
5. If I remove all the DNAPL in a source zone, is there a chance I'll still be above MCLs? How much longer might I have to wait for a source zone to achieve MCLs after the DNAPL is all gone?	Dandy-Sale	Concentration* vs. time plot or mass discharge vs. time plot

* Concentration assuming a monitoring well with a 10-foot screened interval (this cannot be changed in the model)

Which model should I use: SRM or DSM?

I Want the Following Information:	Which Model?	Output
6. I want to make sure the matrix diffusion model accounts for contaminant concentrations in the transmissive zone when calculating the release for low-k zones?	Dandy-Sale	Concentration* vs. time plot or mass discharge vs. time plot

* Concentration assuming a monitoring well with a 10-foot screened interval (this cannot be changed in the model)

Which model should I use: SRM or DSM?

I Want the Following Information:	Which Model?	Output
7. I want to account for the travel time of the plume in the transmissive zone so that the loading period for the downgradient low-k zones starts later than the loading period for the near-source low-k zones. (This is more important for plumes, such as plumes with long residence times, > 20 years).	Dandy-Sale	Concentration* vs. time plot or mass discharge vs. time plot

* Concentration assuming a monitoring well with a 10-foot screened interval (this cannot be changed in the model)

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Model Demo